NPFL122, Lecture 13



Multi-Agent RL, PPO, MAPPO

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unless otherwise stated

Multi-Agent Reinforcement Learning

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We use the thesis

Cooperative Multi-Agent Reinforcement Learning <u>https://dspace.cuni.cz/handle/20.500.11956/127431</u>

as an introduction text.



Multi-Agent Hide-and-Seek

As another example, consider <u>https://openai.com/blog/emergent-tool-use/</u>.



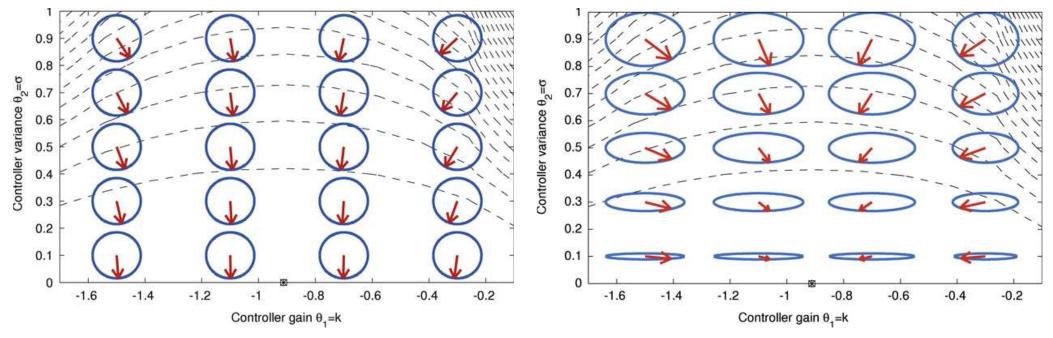
The following approach has been introduced by Kakade (2002).

Using policy gradient theorem, we are able to compute ∇v_{π} . Normally, we update the parameters by using directly this gradient. This choice is justified by the fact that a vector d which maximizes $v_{\pi}(s; \theta + d)$ under the constraint that $|d|^2$ is bounded by a small constant is exactly the gradient ∇v_{π} .

Normally, the length $|\boldsymbol{d}|^2$ is computed using Euclidean metric. But in general, any metric could be used. Representing a metric using a positive-definite matrix \boldsymbol{G} (identity matrix for Euclidean metric), we can compute the distance as $|\boldsymbol{d}|^2 = \sum_{ij} G_{ij} d_i d_j = \boldsymbol{d}^T \boldsymbol{G} \boldsymbol{d}$. The steepest ascent direction is then given by $\boldsymbol{G}^{-1} \nabla v_{\pi}$.

Note that when G is the Hessian Hv_{π} , the above process is exactly Newton's method.





(a) Vanilla policy gradient.

(b) Natural policy gradient. Figure 3 of the paper "Reinforcement learning of motor skills with policy gradients" by Jan Peters et al.

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A suitable choice for the metric is Fisher information matrix defined as

$$F_s(oldsymbol{ heta}) \stackrel{ ext{def}}{=} \mathbb{E}_{\pi(a|s;oldsymbol{ heta})} \left[rac{\partial \log \pi(a|s;oldsymbol{ heta})}{\partial oldsymbol{ heta}_i} rac{\partial \log \pi(a|s;oldsymbol{ heta})}{\partial oldsymbol{ heta}_j}
ight] = \mathbb{E}[
abla \pi(a|s;oldsymbol{ heta})]\mathbb{E}[
abla \pi(a|s;oldsymbol{ heta})]^T.$$

It can be shown that the Fisher information metric is the only Riemannian metric (up to rescaling) invariant to change of parameters under sufficient statistic.

Recall Kullback-Leibler distance (or relative entropy) defined as

$$D_{ ext{KL}}(oldsymbol{p} ||oldsymbol{q}) \stackrel{ ext{def}}{=} \sum_i p_i \log rac{p_i}{q_i} = H(p,q) - H(p).$$

The Fisher information matrix is also a Hessian of the $D_{\mathrm{KL}}(\pi(a|s; \theta) || \pi(a|s; \theta'))$:

$$F_s(oldsymbol{ heta}) = rac{\partial^2}{\partial heta_i' \partial heta_j'} D_{ ext{KL}}(\pi(a|s;oldsymbol{ heta}) || \pi(a|s;oldsymbol{ heta}') \Big|_{oldsymbol{ heta}'=oldsymbol{ heta}}.$$

Using the metric

$$F(oldsymbol{ heta}) = \mathbb{E}_{s \sim \mu_{oldsymbol{ heta}}} F_s(oldsymbol{ heta})$$

we want to update the parameters using $oldsymbol{d}_F \stackrel{\text{\tiny def}}{=} F(oldsymbol{ heta})^{-1}
abla v_\pi.$

An interesting property of using the d_F to update the parameters is that

- updating $\boldsymbol{\theta}$ using $abla v_{\pi}$ will choose an arbitrary *better* action in state s;
- updating $\boldsymbol{\theta}$ using $F(\boldsymbol{\theta})^{-1} \nabla v_{\pi}$ chooses the *best* action (maximizing expected return), similarly to tabular greedy policy improvement.

However, computing d_F in a straightforward way is too costly.

Truncated Natural Policy Gradient

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Duan et al. (2016) in paper Benchmarking Deep Reinforcement Learning for Continuous Control propose a modification to the NPG to efficiently compute d_F .

Following Schulman et al. (2015), they suggest to use *conjugate gradient algorithm*, which can solve a system of linear equations Ax = b in an iterative manner, by using A only to compute products Av for a suitable v.

Therefore, d_F is found as a solution of

$$F(oldsymbol{ heta})oldsymbol{d}_F =
abla v_\pi$$

and using only 10 iterations of the algorithm seem to suffice according to the experiments. Furthermore, Duan et al. suggest to use a specific learning rate suggested by Peters et al (2008) of

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Schulman et al. in 2015 wrote an influential paper introducing TRPO as an improved variant of NPG.

Considering two policies $\pi, \tilde{\pi}$, we can write

$$v_{ ilde{\pi}} = v_{\pi} + \mathbb{E}_{s \sim \mu(ilde{\pi})} \mathbb{E}_{a \sim ilde{\pi}(a|s)} a_{\pi}(a|s),$$

where $a_{\pi}(a|s)$ is the advantage function $q_{\pi}(a|s) - v_{\pi}(s)$ and $\mu(\tilde{\pi})$ is the on-policy distribution of the policy $\tilde{\pi}$.

Analogously to policy improvement, we see that if $a_{\pi}(a|s) \ge 0$, policy $\tilde{\pi}$ performance increases (or stays the same if the advantages are zero everywhere).

However, sampling states $s \sim \mu(ilde{\pi})$ is costly. Therefore, we instead consider

$$L_{\pi}(ilde{\pi}) = v_{\pi} + \mathbb{E}_{s \sim \mu(\pi)} \mathbb{E}_{a \sim ilde{\pi}(a|s)} a_{\pi}(a|s).$$



$$L_{\pi}(ilde{\pi}) = v_{\pi} + \mathbb{E}_{s \sim \mu(\pi)} \mathbb{E}_{a \sim ilde{\pi}(a|s)} a_{\pi}(a|s)$$

It can be shown that for parametrized $\pi(a|s; \theta)$ the $L_{\pi}(\tilde{\pi})$ matches $v_{\tilde{\pi}}$ to the first order.

Schulman et al. additionally proves that if we denote $\alpha = D_{\mathrm{KL}}^{\mathrm{max}}(\pi_{\mathrm{old}} || \pi_{\mathrm{new}}) = \max_{s} D_{\mathrm{KL}}(\pi_{\mathrm{old}}(\cdot |s) || \pi_{\mathrm{new}}(\cdot |s))$, then

$$v_{\pi_{ ext{new}}} \geq L_{\pi_{ ext{old}}}(\pi_{ ext{new}}) - rac{4arepsilon\gamma}{(1-\gamma)^2} lpha ext{ where } arepsilon = \max_{s,a} |a_{\pi}(s,a)|.$$

Therefore, TRPO maximizes $L_{\pi_{\theta_0}}(\pi_{\theta})$ subject to $D_{\mathrm{KL}}^{\theta_0}(\pi_{\theta_0}||\pi_{\theta}) < \delta$, where

- $D_{\mathrm{KL}}^{\theta_0}(\pi_{\theta_0}||\pi_{\theta}) = \mathbb{E}_{s \sim \mu(\pi_{\theta_0})}[D_{\mathrm{KL}}(\pi_{\mathrm{old}}(\cdot|s)||\pi_{\mathrm{new}}(\cdot|s))]$ is used instead of $D_{\mathrm{KL}}^{\mathrm{max}}$ for performance reasons;
- δ is a constant found empirically, as the one implied by the above equation is too small;
- importance sampling is used to account for sampling actions from π .



$$\text{maximize } \ L_{\pi_{\boldsymbol{\theta}_0}}\left(\pi_{\boldsymbol{\theta}}\right) = \mathbb{E}_{s \sim \mu\left(\pi_{\boldsymbol{\theta}_0}\right), a \sim \pi_{\boldsymbol{\theta}_0}\left(a|s\right)} \left[\tfrac{\pi_{\boldsymbol{\theta}}\left(a|s\right)}{\pi_{\boldsymbol{\theta}_0}\left(a|s\right)} a_{\pi_{\boldsymbol{\theta}_0}}\left(a|s\right) \right] \ \text{subject to } \ D_{\text{KL}}^{\boldsymbol{\theta}_0}(\pi_{\boldsymbol{\theta}_0}||\pi_{\boldsymbol{\theta}}) < \delta$$

The parameters are updated using $d_F = F(\theta)^{-1} \nabla L_{\pi_{\theta_0}}(\pi_{\theta})$, utilizing the conjugate gradient algorithm as described earlier for TNPG (note that the algorithm was designed originally for TRPO and only later employed for TNPG).

To guarantee improvement and respect the D_{KL} constraint, a line search is in fact performed. We start by the learning rate of $\sqrt{\delta/(\boldsymbol{d}_F^T F(\boldsymbol{\theta})^{-1} \boldsymbol{d}_F)}$ and shrink it exponentially until the constraint is satistifed and the objective improves.

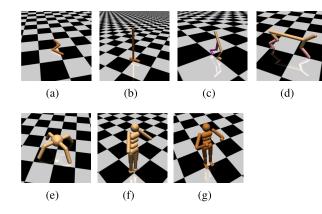


Figure 1. Illustration of locomotion tasks: (a) Swimmer; (b) Hopper; (c) Walker; (d) Half-Cheetah; (e) Ant; (f) Simple Humanoid; and (g) Full Humanoid.

Figure 1 of the paper "Benchmarking Deep Reinforcement Learning for Continuous Control" by Duan et al.

Task	Random	REINFORCE	TNPG	RWR	REPS	TRPO	CEM	CMA-ES	DDPG
Cart-Pole Balancing Inverted Pendulum* Mountain Car Acrobot Double Inverted Pendulum*	$77.1 \pm 0.0 \\ -153.4 \pm 0.2 \\ -415.4 \pm 0.0 \\ -1904.5 \pm 1.0 \\ 149.7 \pm 0.1$	$\begin{array}{rrrr} 4693.7 \pm & 14.0 \\ 13.4 \pm & 18.0 \\ -67.1 \pm & 1.0 \\ -508.1 \pm & 91.0 \\ 4116.5 \pm & 65.2 \end{array}$	$\begin{array}{r} \textbf{3986.4} \ \pm \ \textbf{748.9} \\ \textbf{209.7} \ \pm \ \textbf{55.5} \\ \textbf{-66.5} \ \pm \ \textbf{4.5} \\ \textbf{-395.8} \pm 121.2 \\ \textbf{4455.4} \ \pm \ \textbf{37.6} \end{array}$	$\begin{array}{rrrr} \textbf{4861.5} \ \pm \ \textbf{12.3} \\ 84.7 \pm \ 13.8 \\ -79.4 \pm \ 1.1 \\ -352.7 \pm \ 35.9 \\ 3614.8 \pm 368.1 \end{array}$	$565.6 \pm 137.6 \\ -113.3 \pm 4.6 \\ -275.6 \pm 166.3 \\ -1001.5 \pm 10.8 \\ 446.7 \pm 114.8$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{rrrr} 4815.4 \pm & 4.8 \\ 38.2 \pm & 25.7 \\ -66.0 \pm & 2.4 \\ -436.8 \pm & 14.7 \\ 2566.2 \pm 178.9 \end{array}$	$\begin{array}{rrrr} 2440.4\pm 568.3\\ -40.1\pm & 5.7\\ -85.0\pm & 7.7\\ -785.6\pm & 13.1\\ 1576.1\pm & 51.3\end{array}$	$\begin{array}{r} 4634.4 \ \pm \ 87.8 \\ 40.0 \ \pm \ 244.6 \\ -288.4 \ \pm \ 170.3 \\ \textbf{-223.6} \ \pm \ \textbf{5.8} \\ 2863.4 \ \pm \ 154.0 \end{array}$
Swimmer* Hopper 2D Walker Half-Cheetah Ant* Simple Humanoid Full Humanoid	$-1.7 \pm 0.1 \\ 8.4 \pm 0.0 \\ -1.7 \pm 0.0 \\ -90.8 \pm 0.3 \\ 13.4 \pm 0.7 \\ 41.5 \pm 0.2 \\ 13.2 \pm 0.1$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{rrrr} 64.9 \pm & 1.4 \\ 20.3 \pm & 14.3 \\ 77.1 \pm & 24.3 \\ 441.3 \pm 107.6 \\ 17.8 \pm & 15.5 \\ 28.7 \pm & 3.9 \\ \text{N/A} \pm & \text{N/A} \\ \text{Continuous Contri} \end{array}$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$

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HideAndSeek

NPG

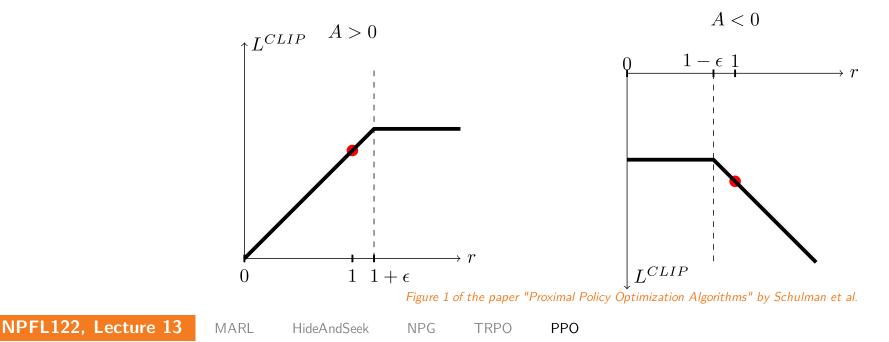
TRPO PPO

Proximal Policy Optimization

A simplification of TRPO which can be implemented using a few lines of code. Let $r_t(\boldsymbol{\theta}) \stackrel{\text{def}}{=} \frac{\pi(A_t|S_t;\boldsymbol{\theta})}{\pi(A_t|S_t;\boldsymbol{\theta}_{\text{old}})}$. PPO maximizes the objective

$$L^{ ext{CLIP}}(oldsymbol{ heta}) \stackrel{ ext{\tiny def}}{=} \mathbb{E}_t \Big[\minig(r_t(oldsymbol{ heta}) \hat{A}_t, ext{clip}(r_t(oldsymbol{ heta}), 1-arepsilon, 1+arepsilon) \hat{A}_t) ig) \Big].$$

Such a $L^{\text{CLIP}}(\boldsymbol{\theta})$ is a lower (pessimistic) bound.



Proximal Policy Optimization

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The advantages \hat{A}_t are additionally estimated using the so-called *generalized advantage* estimation, which is just an analogue of the truncated n-step lambda-return:

$$\hat{A}_t = \sum_{i=0}^{n-1} \gamma^i \lambda^i ig(R_{t+1+i} + \gamma V(S_{t+i+1}) - V(S_{t+i}) ig).$$

Algorithm 1 PPO, Actor-Critic Style

```
for iteration=1,2,..., N do
for actor=1,2,..., N do
Run policy \pi_{\theta_{\text{old}}} in environment for T timesteps
Compute advantage estimates \hat{A}_1, \ldots, \hat{A}_T
end for
Optimize surrogate L wrt \theta, with K epochs and minibatch size M \leq NT
\theta_{\text{old}} \leftarrow \theta
end for
end for
```

Algorithm 1 of the paper "Proximal Policy Optimization Algorithms" by Schulman et al.

Proximal Policy Optimization



Figure 3: Comparison of several algorithms on several MuJoCo environments, training for one million timesteps.

Figure 3 of the paper "Proximal Policy Optimization Algorithms" by Schulman et al.