NPFL122, Lecture 1



Introduction to Reinforcement Learning

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unless otherwise stated

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Develop goal-seeking agent trained using reward signal.

- Optimal control in 1950s Richard Bellman
- Trial and error learning since 1850s
 - $^{\circ}\,$ Law and effect Edward Thorndike, 1911
 - Responses that produce a satisfying effect in a particular situation become more likely to occur again in that situation, and responses that produce a discomforting effect become less likely to occur again in that situation
 - $^{\circ}\,$ Shannon, Minsky, Clark&Farley, ... 1950s and 1960s
 - Tsetlin, Holland, Klopf 1970s
 - $^{\circ}$ Sutton, Barto since 1980s
- Arthur Samuel first implementation of temporal difference methods for playing checkers

Notable successes

- Gerry Tesauro 1992, human-level Backgammon playing program trained solely by self-play
- IBM Watson in Jeopardy 2011

History

Recent successes

- Human-level video game playing (DQN) 2013 (2015 Nature), Mnih. et al, Deepmind
 - 29 games out of 49 comparable or better to professional game players
 - $^{\circ}$ 8 days on GPU
 - $^{\rm O}$ human-normalized mean: 121.9%, median: 47.5% on 57 games
- A3C 2016, Mnih. et al
 - $^{\circ}$ 4 days on 16-threaded CPU
 - $^{\circ}\,$ human-normalized mean: 623.0%, median: 112.6% on 57 games
- Rainbow 2017
 - $^{\circ}\,$ human-normalized median: 153%; ~39 days of game play experience
- Impala Feb 2018
 - $^{\circ}\,$ one network and set of parameters to rule them all
 - $^{\rm O}$ human-normalized mean: 176.9%, median: 59.7% on 57 games
- PopArt-Impala Sep 2018

History

 $^{\circ}$ human-normalized median: 110.7% on 57 games; 57*38.6 days of experience

Recent successes

- R2D2 Jan 2019
 - $^{\circ}\,$ human-normalized mean: 4024.9%, median: 1920.6% on 57 games
 - $^\circ$ processes ~5.7B frames during a day of training
- Data-efficient Rainbow Jun 2019
 - $^{\circ}~$ learning from ${\sim}2$ hours of game experience

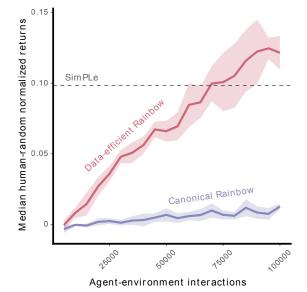
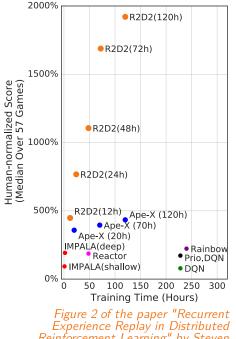


Figure 3 of the paper "When to use parametric models in reinforcement learning?" by Hado van Hasselt et al.



Experience Replay in Distributed Reinforcement Learning" by Steven Kapturowski et al.

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Multi-armed Bandits ε -greedy

Non-stationary Problems

Gradient

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Recent successes

- AlphaGo
 - Mar 2016 beat 9-dan professional player Lee Sedol
- AlphaGo Master Dec 2016

 beat 60 professionals, beat Ke Jie in May 2017
- AlphaGo Zero 2017
 - $^{\rm O}$ trained only using self-play

History

- $^{\circ}$ surpassed all previous version after 40 days of training
- AlphaZero Dec 2017 (Dec 2018 in Nature)
 - self-play only, defeated AlphaGo Zero after 30 hours of training
 - $^{\circ}$ impressive chess and shogi performance after 9h and 12h, respectively

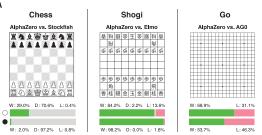


Figure 2 of the paper "A general reinforcement learning algorithm that masters chess, shogi, and Go through self-play" by David Silver et al.

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Recent successes

- Dota2 Aug 2017

 won 1v1 matches against a professional player
- MERLIN Mar 2018
 - $^{\rm O}$ unsupervised representation of states using external memory
 - $^{\circ}\,$ beat human in unknown maze navigation
- FTW Jul 2018
 - $^{\circ}\,$ beat professional players in two-player-team Capture the flag FPS
 - $^{\rm O}$ solely by self-play, trained on 450k games
 - each 5 minutes, 4500 agent steps (15 per second)
- OpenAl Five Aug 2018
 - won 5v5 best-of-three match against professional team
 - $\circ~$ 256 GPUs, 128k CPUs

History

- 180 years of experience per day
- AlphaStar Jan 2019
 - won 10 out of 11 StarCraft II games against two professional players

Recent successes

- Optimize non-differentiable loss
 - $^{\circ}\,$ improved translation quality in 2016
 - $^{\circ}~$ better summarization performance
- Discovering discrete latent structures
- Effectively search in space of natural language policies
- TARDIS Jan 2017
 - $^{\circ}\,$ allow using discrete external memory
- Neural architecture search (Nov 2016)
 - SoTA CNN architecture generated by another network
 - $^{\circ}\,$ can search also for suitable RL architectures, new activation functions, optimizers...

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Comparison



Multi-armed Bandits





http://www.infoslotmachine.com/img/one-armed-bandit.jpg

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History Multi-armed Bandits

 ε -greedy

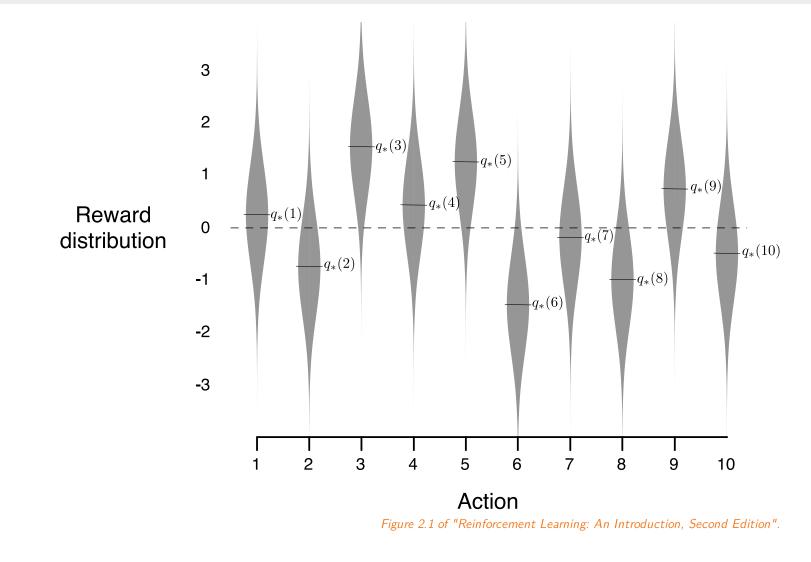
Non-stationary Problems

Gradient

Comparison

Multi-armed Bandits





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We start by selecting action A_1 , which is the index of the arm to use, and we get a reward of R_1 . We then repeat the process by selecting actions A_2 , A_3 , ...

Let $q_*(a)$ be the real value of an action a:

$$q_*(a) = \mathbb{E}[R_t|A_t = a].$$

Denoting $Q_t(a)$ our estimated value of action a at time t (before taking trial t), we would like $Q_t(a)$ to converge to $q_*(a)$. A natural way to estimate $Q_t(a)$ is

 $Q_t(a) \stackrel{ ext{def}}{=} rac{ ext{sum of rewards when action } a ext{ is taken}}{ ext{number of times action } a ext{ was taken}}.$

Following the definition of $Q_t(a)$, we could choose a greedy action A_t as

$$A_t \stackrel{ ext{def}}{=} rg\max_a Q_t(a).$$

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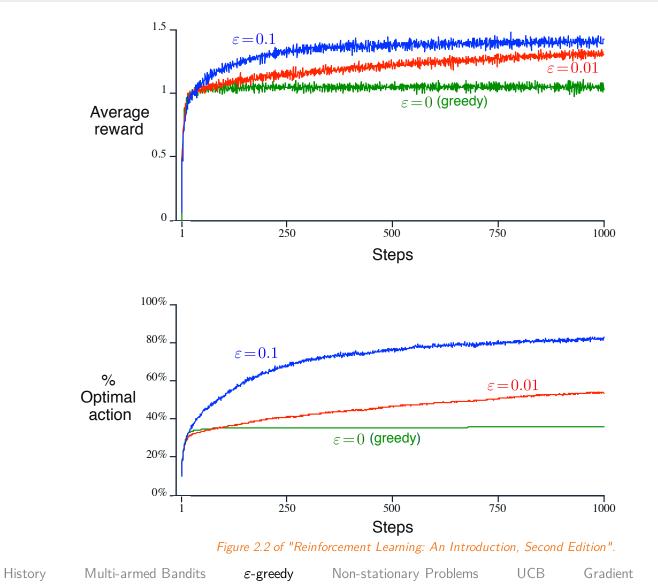
Exploitation versus Exploration

Choosing a greedy action is *exploitation* of current estimates. We however also need to *explore* the space of actions to improve our estimates.

An ε -greedy method follows the greedy action with probability $1 - \varepsilon$, and chooses a uniformly random action with probability ε .

ε -greedy Method

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ε -greedy Method



Incremental Implementation

Let Q_{n+1} be an estimate using n rewards R_1,\ldots,R_n .

$$egin{aligned} Q_{n+1} &= rac{1}{n} \sum_{i=1}^n R_i \ &= rac{1}{n} (R_n + rac{n-1}{n-1} \sum_{i=1}^{n-1} R_i) \ &= rac{1}{n} (R_n + (n-1) Q_n) \ &= rac{1}{n} (R_n + n Q_n - Q_n) \ &= Q_n + rac{1}{n} \Big(R_n - Q_n \Big) \end{aligned}$$

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Gradient

ε -greedy Method Algorithm

A simple bandit algorithm

```
Initialize, for a = 1 to k:
      Q(a) \leftarrow 0
      N(a) \leftarrow 0
Loop forever:
      A \leftarrow \begin{cases} \operatorname{argmax}_{a} Q(a) & \text{with probability } 1 - \varepsilon \\ \operatorname{a random action} & \text{with probability } \varepsilon \end{cases}
      R \leftarrow bandit(A)
```

$$N(A) \leftarrow N(A) + 1$$

$$Q(A) \leftarrow Q(A) + \frac{1}{N(A)} \left[R - Q(A) \right]$$

Algorithm 2.4 of "Reinforcement Learning: An Introduction, Second Edition".

(breaking ties randomly)

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Fixed Learning Rate



Analogously to the solution obtained for a stationary problem, we consider

$$Q_{n+1}=Q_n+lpha(R_n-Q_n).$$

Converges to the true action values if

$$\sum_{n=1}^\infty lpha_n = \infty \quad ext{and} \quad \sum_{n=1}^\infty lpha_n^2 < \infty.$$

Biased method, because

$$Q_{n+1}=(1-lpha)^nQ_1+\sum_{i=1}^nlpha(1-lpha)^{n-i}R_i.$$

The bias can be utilized to support exploration at the start of the episode by setting the initial values to more than the expected value of the optimal solution.

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Optimistic Initial Values and Fixed Learning Rate

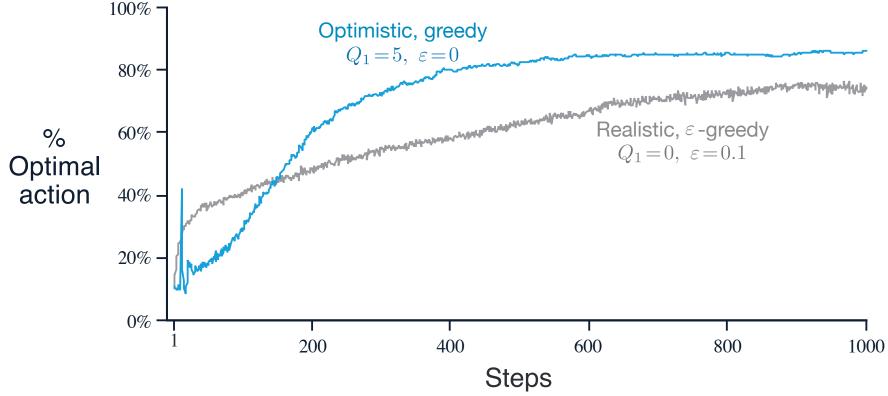


Figure 2.3 of "Reinforcement Learning: An Introduction, Second Edition".

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Upper Confidence Bound



Using same epsilon for all actions in ε -greedy method seems inefficient. One possible improvement is to select action according to upper confidence bound (instead of choosing a random action with probability ε):

$$A_t \stackrel{ ext{def}}{=} rg\max_a \left[Q_t(a) + c \sqrt{rac{\ln t}{N_t(a)}}
ight].$$

The updates are then performed as before (e.g., using averaging, or fixed learning rate α). Note that if $N_t(a) = 0$, the right expression is assumed to have a value of ∞ .

History

Motivation Behind Upper Confidence Bound

Actions with little average reward are probably selected too often.

Instead of simple ε -greedy approach, we might try selecting an action as little as possible, but still enough to converge.

Assuming random variables X_i bounded by [0,1] and $\bar{X} = \sum_{i=1}^N X_i$, (Chernoff-)Hoeffding's inequality states that

$$P(ar{X} - \mathbb{E}[ar{X}] \geq \delta) \leq e^{-2n\delta^2}$$

Our goal is to choose δ such that for every action,

$$P(Q_t(a)-q_*(a)\geq \delta)\leq \left(rac{1}{t}
ight)^lpha.$$

We can achieve the required inequality (with lpha=2) by setting

$$\delta \geq \sqrt{(\ln t)/N_t(a)}.$$

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Asymptotical Optimality of UCB

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We define *regret* as a difference of maximum of what we could get (i.e., repeatedly using action with maximum expectation) and what a strategy yields, i.e.,

$$\mathit{regret}_N \stackrel{\scriptscriptstyle{ ext{def}}}{=} N \max_a q_*(a) - \sum_{i=1}^N \mathbb{E}[R_i].$$

It can be shown that regret of UCB is asymptotically optimal, see Lai and Robbins (1985), Asymptotically Efficient Adaptive Allocation Rules.

Upper Confidence Bound Results



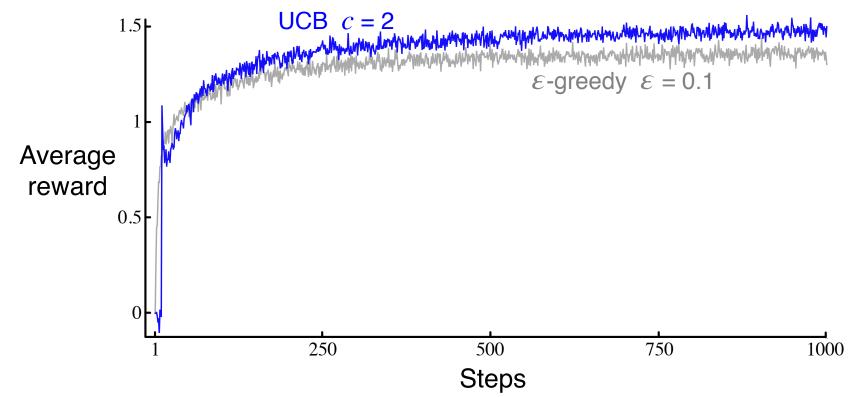


Figure 2.4 of "Reinforcement Learning: An Introduction, Second Edition".

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Gradient Bandit Algorithms

Let $H_t(a)$ be a numerical *preference* for an action a at time t.

We could choose actions according to softmax distribution:

$$\pi(A_t=a) \stackrel{ ext{def}}{=} \operatorname{softmax}(a) = rac{e^{H_t(a)}}{\sum_b e^{H_t(b)}}.$$

In other words, we model a *distribution* of the most rewarding action.

Usually, all $H_1(a)$ are set to zero, which corresponds to random uniform initial policy. Using SGD and MLE loss, we can (and later we will) derive the following algorithm:

$$H_{t+1}(a) \leftarrow H_t(a) + lpha R_t([a=A_t]-\pi(a)).$$

The $[a = A_t]$ is a one-hot vector with the element corresponding to action A_t set to 1.



Gradient Bandit Algorithms



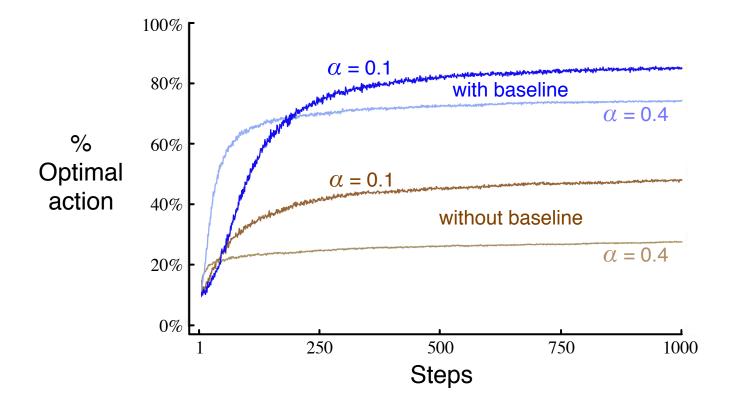


Figure 2.5: Average performance of the gradient bandit algorithm with and without a reward baseline on the 10-armed testbed when the $q_*(a)$ are chosen to be near +4 rather than near zero. Figure 2.5 of "Reinforcement Learning: An Introduction, Second Edition".

Method Comparison



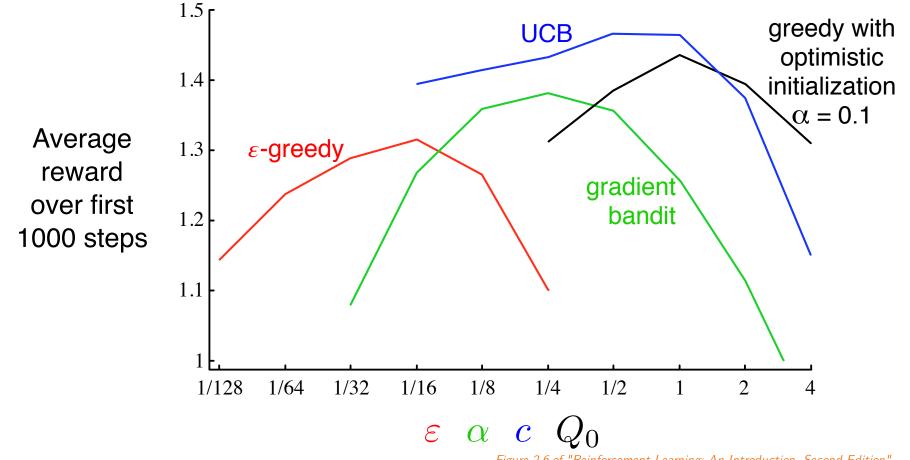


Figure 2.6 of "Reinforcement Learning: An Introduction, Second Edition".

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