NPFL114, Lecture 12



Deep Reinforcement Learning, VAE

Milan Straka

i ∰ May 2, 2023





EUROPEAN UNION European Structural and Investment Fund Operational Programme Research, Development and Education Charles University in Prague Faculty of Mathematics and Physics Institute of Formal and Applied Linguistics



unless otherwise stated



Reinforcement Learning

NPFL114, Lecture 12

MABandits

RL

REINFORCE

MDP

Baseline N

NAS RLWhatNext

GenerativeModels

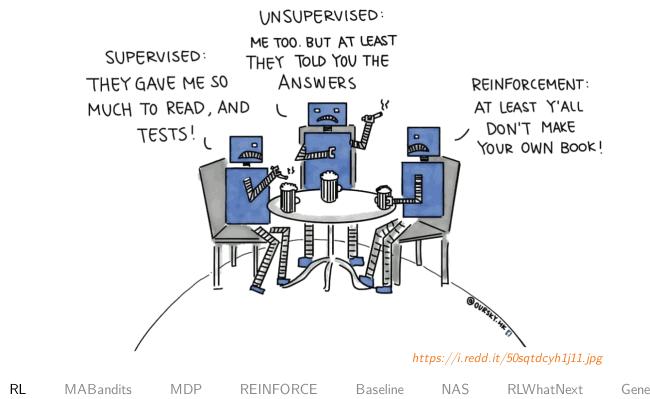
VAE

Reinforcement Learning

NPFL114, Lecture 12

Reinforcement learning is a machine learning paradigm, different from *supervised* and *unsupervised learning*.

The essence of reinforcement learning is to learn from *interactions* with the environment to maximize a numeric *reward* signal. The learner is not told which actions to take, and the actions may affect not just the immediate reward, but also all following rewards.



GenerativeModels VAE

History of Reinforcement Learning

Ú FAL

Develop goal-seeking agent trained using reward signal.

- Optimal control in 1950s Richard Bellman
- Trial and error learning since 1850s
 - $^{\circ}\,$ Law and effect Edward Thorndike, 1911
 - Responses that produce a satisfying effect in a particular situation become more likely to occur again in that situation, and responses that produce a discomforting effect become less likely to occur again in that situation
 - $^{\circ}\,$ Shannon, Minsky, Clark&Farley, ... 1950s and 1960s
 - Tsetlin, Holland, Klopf 1970s
 - Sutton, Barto since 1980s

Reinforcement Learning Successes

NPFL114, Lecture 12

RL

MABandits

- Human-level video game playing (DQN) 2013 (2015 Nature), Mnih. et al, Deepmind.
 - After 7 years of development, the Agent57 beats humans on all 57 Atari 2600 games, achieving a mean score of 4766% compared to human players.
- AlphaGo beat 9-dan professional player Lee Sedol in Go in Mar 2016.
 After two years of development, AlphaZero achieved best performance in Go, chess, shogi, being trained using self-play only.

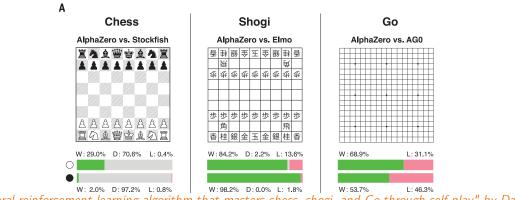


Figure 2 of "A general reinforcement learning algorithm that masters chess, shogi, and Go through self-play" by David Silver et al.

Baseline

NAS

RLWhatNext

GenerativeModels

• Impressive performance in Dota2, Capture the flag FPS, StarCraft II, ...

REINFORCE

MDP

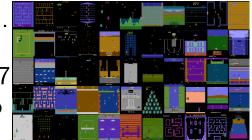


Figure 1 of "A Comparison of learning algorithms on the Arcade Learning Environment", https://arxiv.org/abs/1410.8620

VAE

Reinforcement Learning Successes

- Neural Architecture Search since 2017
 - automatically designing CNN image recognition networks surpassing state-of-the-art performance
 - NasNet, EfficientNet, EfficientNetV2, ...
 - AutoML: automatically discovering
 - architectures (CNN, RNN, overall topology)
 - activation functions
 - optimizers
 - **.**..

NPFL114, Lecture 12

Optimize nondifferentiable loss

 improved translation quality in 2016

MABandits

• Discovering discrete latent structures

RL

Controlling cooling in Google datacenters directly by AI (2018)
 reaching 30% cost reduction

MDP

• Reinforcement learning from human feedback (RLHF) is used during ChatGPT training.

Baseline

NAS

RLWhatNext

REINFORCE

VAE

GenerativeModels

Multi-armed Bandits





http://www.infoslotmachine.com/img/one-armed-bandit.jpg

NPFL114, Lecture 12

MABandits

RL

REINFORCE

MDP

Baseline

NAS

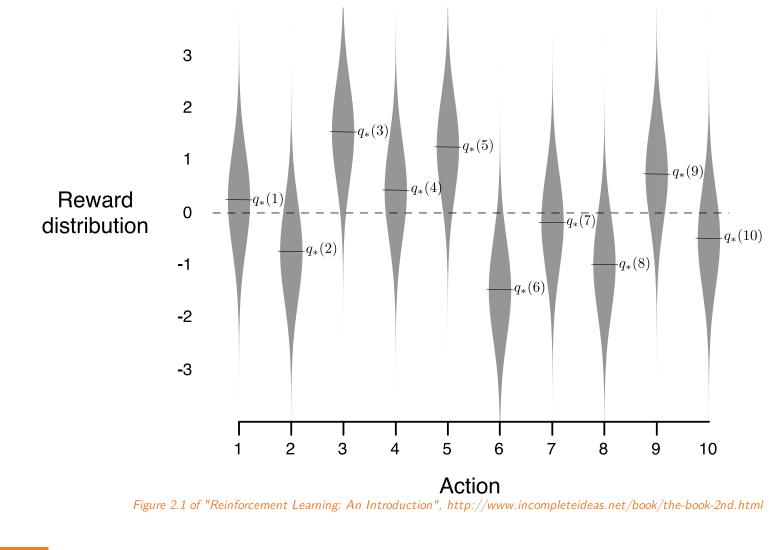
RLWhatNext

GenerativeModels

s VAE

Multi-armed Bandits





NPFL114, Lecture 12 RL

MABandits

MDP REINFORCE

Baseline

NAS RLWhatNext

GenerativeModels

8/56

VAE

Multi-armed Bandits

We start by selecting action A_1 , which is the index of the arm to use, and we get a reward of R_1 . We then repeat the process by selecting actions A_2 , A_3 , ...

Let $q_*(a)$ be the real **value** of an action a:

$$q_*(a) = \mathbb{E}[R_t|A_t = a].$$

Denoting $Q_t(a)$ our estimated value of action a at time t (before taking trial t), we would like $Q_t(a)$ to converge to $q_*(a)$. A natural way to estimate $Q_t(a)$ is

 $Q_t(a) \stackrel{ ext{def}}{=} rac{ ext{sum of rewards when action } a ext{ is taken}}{ ext{number of times action } a ext{ was taken}}.$

Following the definition of $Q_t(a)$, we could choose a greedy action A_t as

$$A_t \stackrel{ ext{def}}{=} rg\max_a Q_t(a).$$





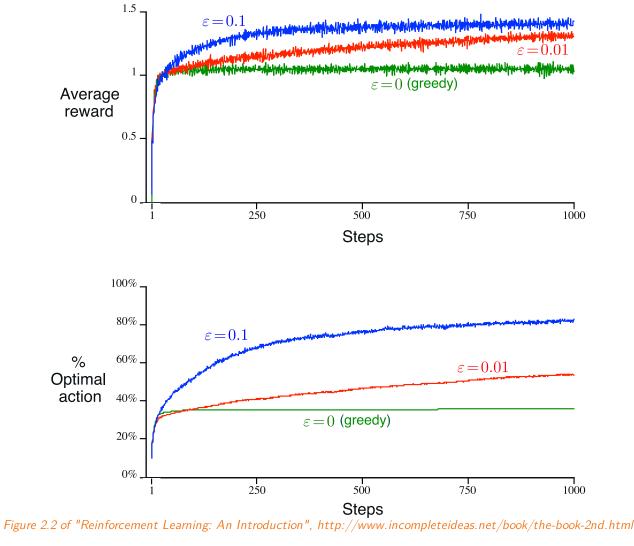
Exploitation versus Exploration

Choosing a greedy action is **exploitation** of current estimates. We however also need to **explore** the space of actions to improve our estimates.

An ε -greedy method follows the greedy action with probability $1 - \varepsilon$, and chooses a uniformly random action with probability ε .

ε -greedy Method

NPFL114, Lecture 12



MABandits MDP

RL

REINFORCE

Baseline

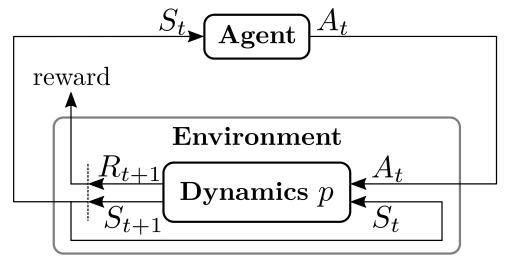
NAS

RLWhatNext GenerativeModels 11/56

VAE

Markov Decision Process





A Markov decision process (MDP) is a quadruple $(\mathcal{S}, \mathcal{A}, p, \gamma)$, where:

- \mathcal{S} is a set of states.
- \mathcal{A} is a set of actions.
- $p(S_{t+1} = s', R_{t+1} = r | S_t = s, A_t = a)$ is a probability that action $a \in \mathcal{A}$ will lead from state $s \in \mathcal{S}$ to $s' \in \mathcal{S}$, producing a reward $r \in \mathbb{R}$,
- $\gamma \in [0,1]$ is a **discount factor** (we always use $\gamma = 1$ and finite episodes in this course).

Let a **return** G_t be $G_t \stackrel{\text{\tiny def}}{=} \sum_{k=0}^{\infty} \gamma^k R_{t+1+k}$. The goal is to optimize $\mathbb{E}[G_0]$.

REINFORCE

Episodic and Continuing Tasks

If the agent-environment interaction naturally breaks into independent subsequences, usually called **episodes**, we talk about **episodic tasks**. Each episode then ends in a special **terminal state**, followed by a reset to a starting state (either always the same, or sampled from a distribution of starting states).

In episodic tasks, it is often the case that every episode ends in at most H steps. These **finite-horizon tasks** then can use discount factor $\gamma = 1$, because the return $G \stackrel{\text{def}}{=} \sum_{t=0}^{H} \gamma^t R_{t+1}$ is well defined.

If the agent-environment interaction goes on and on without a limit, we instead talk about continuing tasks. In this case, the discount factor γ needs to be sharply smaller than 1.

VAE

A **policy** π computes a distribution of actions in a given state, i.e., $\pi(a|s)$ corresponds to a probability of performing an action a in state s.

We will model a policy using a neural network with parameters $\boldsymbol{\theta}$:

 $\pi(a|s; \boldsymbol{\theta}).$

If the number of actions is finite, we consider the policy to be a categorical distribution and utilize the softmax output activation as in supervised classification.

(State-)Value and Action-Value Functions

Ú_F≩L

To evaluate a quality of a policy, we define value function $v_{\pi}(s)$, or state-value function, as

$$egin{aligned} v_{\pi}(s) \stackrel{ ext{def}}{=} \mathbb{E}_{\pi} \left[G_t | S_t = s
ight] = \mathbb{E}_{\pi} \left[\sum_{k=0}^{\infty} \gamma^k R_{t+k+1} \Big| S_t = s
ight] \ &= \mathbb{E}_{A_t \sim \pi(s)} \mathbb{E}_{S_{t+1}, R_{t+1} \sim p(s, A_t)} \left[R_{t+1} + \gamma \mathbb{E}_{A_{t+1} \sim \pi(S_{t+1})} \mathbb{E}_{S_{t+2}, R_{t+2} \sim p(S_{t+1}, A_{t+1})} \left[R_{t+2} + \dots
ight]
ight] \end{aligned}$$

An action-value function for a policy π is defined analogously as

$$q_{\pi}(s,a) \stackrel{\scriptscriptstyle\mathrm{def}}{=} \mathbb{E}_{\pi}\left[G_t|S_t=s,A_t=a
ight] = \mathbb{E}_{\pi}\left[\sum_{k=0}^{\infty}\gamma^k R_{t+k+1}\Big|S_t=s,A_t=a
ight].$$

The value function and the state-value function can be easily expressed using one another:

$$egin{aligned} v_\pi(s) &= \mathbb{E}_{a \sim \pi}ig[q_\pi(s,a)ig], \ q_\pi(s,a) &= \mathbb{E}_{s',r \sim p}ig[r+\gamma v_\pi(s')ig]. \end{aligned}$$

NPFL114, Lecture 12

RL

REINFORCE

Baseline NAS

GenerativeModels

VAE

Optimal Value Functions



Optimal state-value function is defined as

$$v_*(s) \stackrel{ ext{\tiny def}}{=} \max_\pi v_\pi(s),$$

and **optimal action-value function** is defined analogously as

$$q_*(s,a) \stackrel{ ext{\tiny def}}{=} \max_\pi q_\pi(s,a).$$

Any policy π_* with $v_{\pi_*} = v_*$ is called an **optimal policy**. Such policy can be defined as $\pi_*(s) \stackrel{\text{def}}{=} rg\max_a q_*(s, a) = rg\max_a \mathbb{E}[R_{t+1} + \gamma v_*(S_{t+1})|S_t = s, A_t = a]$. When multiple actions maximize $q_*(s, a)$, the optimal policy can stochastically choose any of them.

Existence

In finite-horizon tasks or if $\gamma < 1$, there always exists a unique optimal state-value function, a unique optimal action-value function, and a (not necessarily unique) optimal policy.

Policy Gradient Methods

We train the policy

 $\pi(a|s;oldsymbol{ heta})$

```
by maximizing the expected return v_{\pi}(s).
```

To that account, we need to compute its gradient $\nabla_{\theta} v_{\pi}(s)$.



Policy Gradient Theorem

Assume that S and A are finite, $\gamma = 1$, and that maximum episode length H is also finite. Let $\pi(a|s; \theta)$ be a parametrized policy. We denote the initial state distribution as h(s) and the on-policy distribution under π as $\mu(s)$. Let also $J(\theta) \stackrel{\text{def}}{=} \mathbb{E}_{s \sim h} v_{\pi}(s)$.

Then

$$abla_{oldsymbol{ heta}} v_{\pi}(s) \propto \sum_{s' \in \mathcal{S}} P(s
ightarrow \ldots
ightarrow s' | \pi) \sum_{a \in \mathcal{A}} q_{\pi}(s',a)
abla_{oldsymbol{ heta}} \pi(a|s';oldsymbol{ heta})$$

and

$$abla_{oldsymbol{ heta}} J(oldsymbol{ heta}) \propto \sum_{s \in \mathcal{S}} \mu(s) \sum_{a \in \mathcal{A}} q_{\pi}(s,a)
abla_{oldsymbol{ heta}} \pi(a|s;oldsymbol{ heta}),$$

where $P(s \to ... \to s' | \pi)$ is the probability of getting to state s' when starting from state s, after any number of 0, 1, ... steps.

Proof of Policy Gradient Theorem

$$\begin{split} \nabla v_{\pi}(s) &= \nabla \Big[\sum_{a} \pi(a|s; \boldsymbol{\theta}) q_{\pi}(s, a) \Big] \\ &= \sum_{a} \Big[q_{\pi}(s, a) \nabla \pi(a|s; \boldsymbol{\theta}) + \pi(a|s; \boldsymbol{\theta}) \nabla q_{\pi}(s, a) \Big] \\ &= \sum_{a} \Big[q_{\pi}(s, a) \nabla \pi(a|s; \boldsymbol{\theta}) + \pi(a|s; \boldsymbol{\theta}) \nabla \big(\sum_{s', r} p(s', r|s, a)(r + v_{\pi}(s')) \big) \Big] \\ &= \sum_{a} \Big[q_{\pi}(s, a) \nabla \pi(a|s; \boldsymbol{\theta}) + \pi(a|s; \boldsymbol{\theta}) \big(\sum_{s'} p(s'|s, a) \nabla v_{\pi}(s') \big) \Big] \end{split}$$

 We now expand $v_{\pi}(s')$.

$$=\sum_{a}\left[q_{\pi}(s,a)
abla\pi(a|s;oldsymbol{ heta})+\pi(a|s;oldsymbol{ heta})iggl(\sum_{s'}p(s'|s,a)iggl(\sum_{s''}p(s''|s',a')
abla v_{\pi}(s'')iggr)iggr)iggr)iggr)
ight] \\ \sum_{a'}\left[q_{\pi}(s',a')
abla\pi(a'|s';oldsymbol{ heta})+\pi(a'|s';oldsymbol{ heta})iggl(\sum_{s''}p(s''|s',a')
abla v_{\pi}(s'')iggr)iggr)iggr)iggr)iggr)iggr)iggr)$$

Continuing to expand all $v_{\pi}(s'')$, we obtain the following:

$$\nabla v_{\pi}(s) = \sum_{\substack{s' \in \mathcal{S} \\ \text{RL}}} \sum_{\substack{k=0 \\ \text{RL}}}^{H} P(s \to s' \text{ in } k \text{ steps } | \pi) \sum_{\substack{a \in \mathcal{A} \\ \text{Baseline}}} q_{\pi}(s', a) \nabla_{\theta} \pi(a | s'; \theta).$$
PFL114, Lecture 12 RL MABandits MDP REINFORCE Baseline NAS RLWhatNext GenerativeModels VAE 19/56

Proof of Policy Gradient Theorem



To finish the proof of the first part, it is enough to realize that

$$\sum_{k=0}^{H} P(s
ightarrow s' ext{ in } k ext{ steps } |\pi) \propto P(s
ightarrow \ldots
ightarrow s' |\pi).$$

For the second part, we know that

$$abla_{oldsymbol{ heta}} J(oldsymbol{ heta}) = \mathbb{E}_{s \sim h}
abla_{oldsymbol{ heta}} v_{\pi}(s) \propto \mathbb{E}_{s \sim h} \sum_{s' \in \mathcal{S}} P(s
ightarrow \ldots
ightarrow s'|\pi) \sum_{a \in \mathcal{A}} q_{\pi}(s',a)
abla_{oldsymbol{ heta}} \pi(a|s';oldsymbol{ heta}),$$

therefore using the fact that $\mu(s') = \mathbb{E}_{s \sim h} P(s
ightarrow \ldots
ightarrow s' | \pi)$ we get

$$abla_{oldsymbol{ heta}} J(oldsymbol{ heta}) \propto \sum_{s \in \mathcal{S}} \mu(s) \sum_{a \in \mathcal{A}} q_{\pi}(s,a)
abla_{oldsymbol{ heta}} \pi(a|s;oldsymbol{ heta}).$$

Finally, note that the theorem can be proven with infinite S and A; and also for infinite episodes when discount factor $\gamma < 1$.

REINFORCE Algorithm

Ú F_AL

The REINFORCE algorithm (Williams, 1992) uses directly the policy gradient theorem, minimizing $-J(\theta) \stackrel{\text{\tiny def}}{=} -\mathbb{E}_{s\sim h} v_{\pi}(s)$. The loss gradient is then

$$abla_{oldsymbol{ heta}} - J(oldsymbol{ heta}) \propto -\sum_{s\in\mathcal{S}} \mu(s) \sum_{a\in\mathcal{A}} q_{\pi}(s,a)
abla_{oldsymbol{ heta}} \pi(a|s;oldsymbol{ heta}) = -\mathbb{E}_{s\sim\mu} \sum_{a\in\mathcal{A}} q_{\pi}(s,a)
abla_{oldsymbol{ heta}} \pi(a|s;oldsymbol{ heta}).$$

However, the sum over all actions is problematic. Instead, we rewrite it to an expectation which we can estimate by sampling:

$$abla_{oldsymbol{ heta}} - J(oldsymbol{ heta}) \propto \mathbb{E}_{s \sim \mu} \mathbb{E}_{a \sim \pi} q_{\pi}(s, a)
abla_{oldsymbol{ heta}} - \log \pi(a|s; oldsymbol{ heta}),$$

where we used the fact that

RL

$$abla_{oldsymbol{ heta}} \log \pi(a|s;oldsymbol{ heta}) = rac{1}{\pi(a|s;oldsymbol{ heta})}
abla_{oldsymbol{ heta}} \pi(a|s;oldsymbol{ heta}).$$

NPFL114, Lecture 12

REINFORCE

Baseline NAS

VAE 21/56

REINFORCE Algorithm



REINFORCE therefore minimizes the loss $-J(\boldsymbol{\theta})$ with gradient

$$\mathbb{E}_{s\sim\mu}\mathbb{E}_{a\sim\pi}q_{\pi}(s,a)
abla_{oldsymbol{ heta}}-\log\pi(a|s;oldsymbol{ heta}),$$

where we estimate the $q_{\pi}(s, a)$ by a single sample.

Note that the loss is just a weighted variant of negative log-likelihood (NLL), where the sampled actions play a role of gold labels and are weighted according to their return.

REINFORCE: Monte-Carlo Policy-Gradient Control (episodic) for π_*

```
Input: a differentiable policy parameterization \pi(a|s, \theta)

Algorithm parameter: step size \alpha > 0

Initialize policy parameter \theta \in \mathbb{R}^{d'} (e.g., to 0)

Loop forever (for each episode):

Generate an episode S_0, A_0, R_1, \dots, S_{T-1}, A_{T-1}, R_T, following \pi(\cdot|\cdot, \theta)

Loop for each step of the episode t = 0, 1, \dots, T - 1:

G \leftarrow \sum_{k=t+1}^T \gamma^{k-t-1} R_k

\theta \leftarrow \theta + \alpha G \nabla \ln \pi(A_t|S_t, \theta)
(G<sub>t</sub>)
```

Modified from Algorithm 13.3 of "Reinforcement Learning: An Introduction", http://www.incompleteideas.net/book/the-book-2nd.html by removing γ t from the update of θ

REINFORCE Algorithm Example Performance

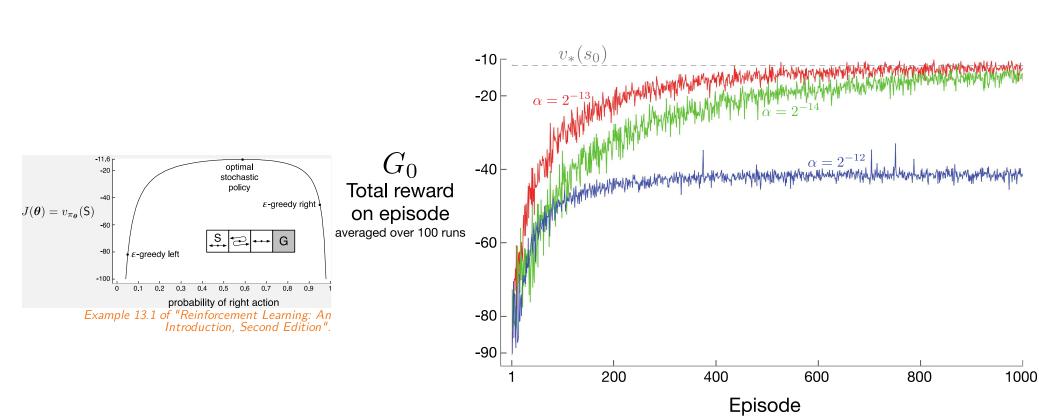


Figure 13.1 of "Reinforcement Learning: An Introduction, Second Edition".

NPFL114, Lecture 12

MABandits

RL

REINFORCE MDP

Baseline

NAS

RLWhatNext

VAE GenerativeModels

REINFORCE with Baseline

The returns can be arbitrary – better-than-average and worse-than-average returns cannot be recognized from the absolute value of the return.

Hopefully, we can generalize the policy gradient theorem using a baseline b(s) to

$$abla_{oldsymbol{ heta}} J(oldsymbol{ heta}) \propto \sum_{s \in \mathcal{S}} \mu(s) \sum_{a \in \mathcal{A}} ig(q_{\pi}(s,a) - b(s) ig)
abla_{oldsymbol{ heta}} \pi(a|s;oldsymbol{ heta}).$$

The baseline b(s) can be a function or even a random variable, as long as it does not depend on a, because

$$\sum_a b(s)
abla_{oldsymbol{ heta}} \pi(a|s;oldsymbol{ heta}) = b(s) \sum_a
abla_{oldsymbol{ heta}} \pi(a|s;oldsymbol{ heta}) = b(s)
abla_{oldsymbol{ heta}} \sum_a \pi(a|s;oldsymbol{ heta}) = b(s)
abla_{oldsymbol{ heta}} 1 = 0.$$

NPFL114, Lecture 12

RL

REINFORCE

Baseline NAS

odels VAE 24/



REINFORCE with Baseline

A good choice for b(s) is $v_{\pi}(s)$, which can be shown to minimize the variance of the gradient estimator. Such baseline reminds centering of the returns, given that

$$v_{\pi}(s) = \mathbb{E}_{a \sim \pi} q_{\pi}(s,a).$$

Then, better-than-average returns are positive and worse-than-average returns are negative. The resulting $q_{\pi}(s, a) - v_{\pi}(s)$ function is also called the **advantage** function

$$a_\pi(s,a) \stackrel{ ext{\tiny def}}{=} q_\pi(s,a) - v_\pi(s).$$

Of course, the $v_{\pi}(s)$ baseline can be only approximated. If neural networks are used to estimate $\pi(a|s; \theta)$, then some part of the network is usually shared between the policy and value function estimation, which is trained using mean square error of the predicted and observed return.



Input: a differentiable policy parameterization $\pi(a|s, \theta)$ Input: a differentiable state-value function parameterization $\hat{v}(s, \mathbf{w})$ Algorithm parameters: step sizes $\alpha^{\theta} > 0, \ \alpha^{\mathbf{w}} > 0$ Initialize policy parameter $\boldsymbol{\theta} \in \mathbb{R}^{d'}$ and state-value weights $\mathbf{w} \in \mathbb{R}^{d}$ (e.g., to **0**) Loop forever (for each episode): Generate an episode $S_0, A_0, R_1, \ldots, S_{T-1}, A_{T-1}, R_T$, following $\pi(\cdot | \cdot, \theta)$ Loop for each step of the episode $t = 0, 1, \ldots, T - 1$: $G \leftarrow \sum_{k=t+1}^{T} \gamma^{k-t-1} R_k$ (G_{t}) $\delta \leftarrow G - \hat{v}(S_t, \mathbf{w})$ $\mathbf{w} \leftarrow \mathbf{w} + \alpha^{\mathbf{w}} \delta \nabla \hat{v}(S_t, \mathbf{w})$ $\boldsymbol{\theta} \leftarrow \boldsymbol{\theta} + \alpha^{\boldsymbol{\theta}} \delta \nabla \ln \pi (A_t | S_t, \boldsymbol{\theta})$

Modified from Algorithm 13.4 of "Reinforcement Learning: An Introduction", http://www.incompleteideas.net/book/the-book-2nd.html by removing γ^{t} from the update of θ

NPFL114, Lecture 12

MABandits

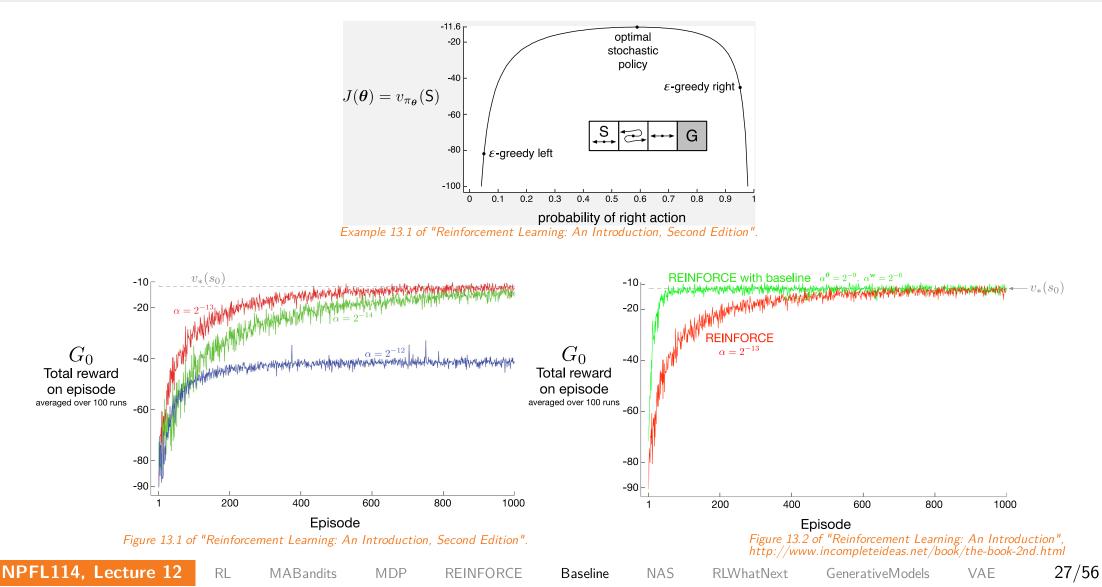
RL

MDP REINFORCE

Baseline NAS



REINFORCE with Baseline Example Performance



NPFL114, Lecture 12

RL

MABandits

MDP

- We can design neural network architectures using reinforcement learning.
- The designed network is encoded as a sequence of elements, and is generated using an **RNN controller**, which is trained using the REINFORCE with baseline algorithm.

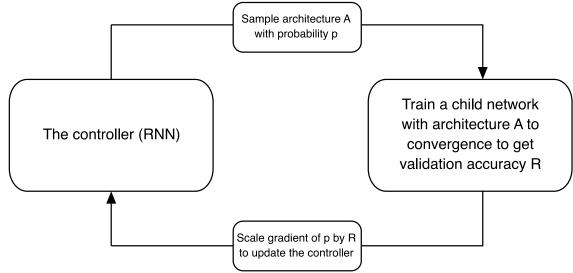


Figure 1 of "Learning Transferable Architectures for Scalable Image Recognition", https://arxiv.org/abs/1707.07012

• For every generated sequence, the corresponding network is trained on CIFAR-10 and the development accuracy is used as a return.

GenerativeModels VAE



The overall architecture of the designed network is fixed and only the Normal Cells and Reduction Cells are generated by the controller.

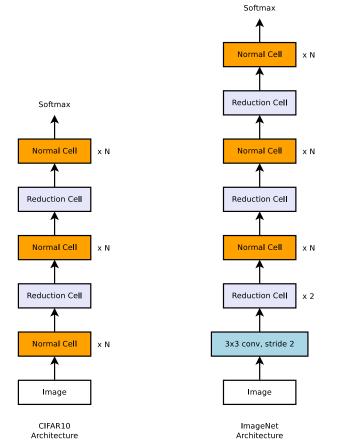


Figure 2 of "Learning Transferable Architectures for Scalable Image Recognition", https://arxiv.org/abs/1707.07012

NPFL114, Lecture 12

RL

MABandits

MDP

REINFORCE

Baseline

NAS

RLWhatNext

GenerativeModels VAE

- Each cell is composed of B blocks (B = 5 is used in NASNet).
- Each block is designed by a RNN controller generating 5 parameters.

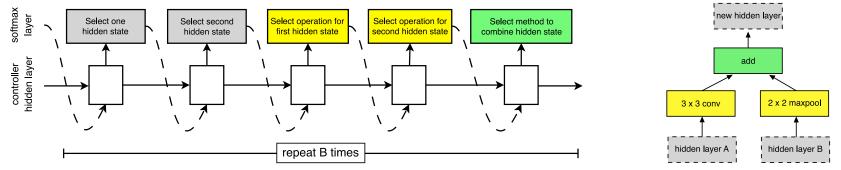


Figure 3. Controller model architecture for recursively constructing one block of a convolutional cell. Each block requires selecting 5 discrete parameters, each of which corresponds to the output of a softmax layer. Example constructed block shown on right. A convolutional cell contains B blocks, hence the controller contains 5B softmax layers for predicting the architecture of a convolutional cell. In our experiments, the number of blocks B is 5.

Figure 3 of "Learning Transferable Architectures for Scalable Image Recognition", https://arxiv.org/abs/1707.07012

- **Step 1.** Select a hidden state from h_i, h_{i-1} or from the set of hidden states created in previous blocks.
- Step 2. Select a second hidden state from the same options as in Step 1.
- Step 3. Select an operation to apply to the hidden state selected in Step 1.
- Step 4. Select an operation to apply to the hidden state selected in Step 2.
- Step 5. Select a method to combine the outputs of Step 3 and 4 to create a new hidden state.

Page 3 of "Learning Transferable Architectures for Scalable Image Recognition", https://arxiv.org/abs/1707.07012

MDP

- identity
- 1x7 then 7x1 convolution
- 3x3 average pooling
- 5x5 max pooling
- 1x1 convolution
- 3x3 depthwise-separable conv
- 7x7 depthwise-separable conv

- 1x3 then 3x1 convolution
- 3x3 dilated convolution
- 3x3 max pooling
- 7x7 max pooling
- 3x3 convolution
- 5x5 depthwise-seperable conv

Figure 2 of "Learning Transferable Architectures for Scalable Image Recognition", https://arxiv.org/abs/1707.07012

NPFL114. Lecture 12

MABandits

RL

REINFORCE

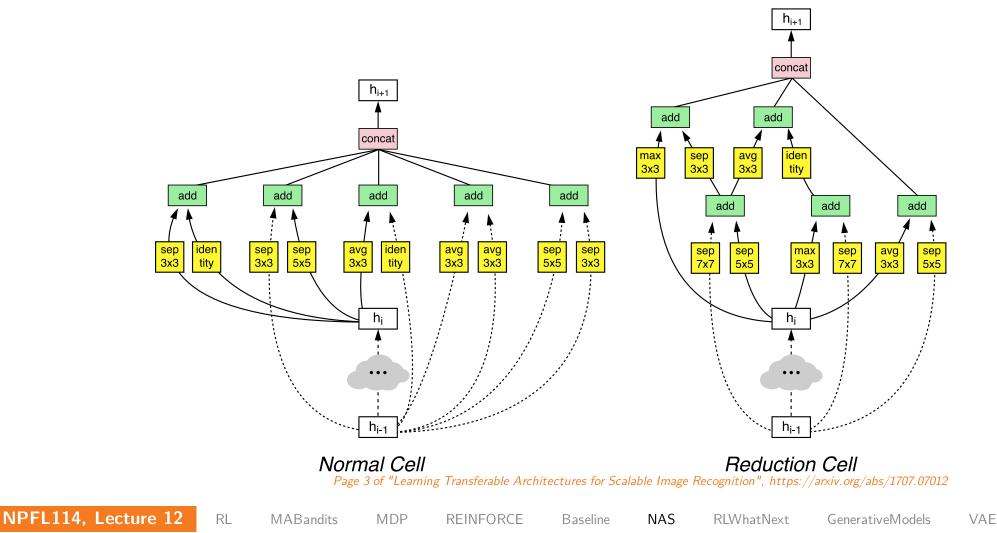
NAS Baseline

RLWhatNext

GenerativeModels VAE



The final Normal Cell and Reduction Cell chosen from 20k architectures (500GPUs, 4days).



EfficientNet Search

Ú F_ÁL

EfficientNet changes the search in three ways.

• Computational requirements are part of the return. Notably, the goal is to find an architecture m maximizing

$$ext{DevelopmentAccuracy}(m) \cdot \left(rac{ ext{TargetFLOPS}=400 ext{M}}{ ext{FLOPS}(m)}
ight)^{0.07},$$

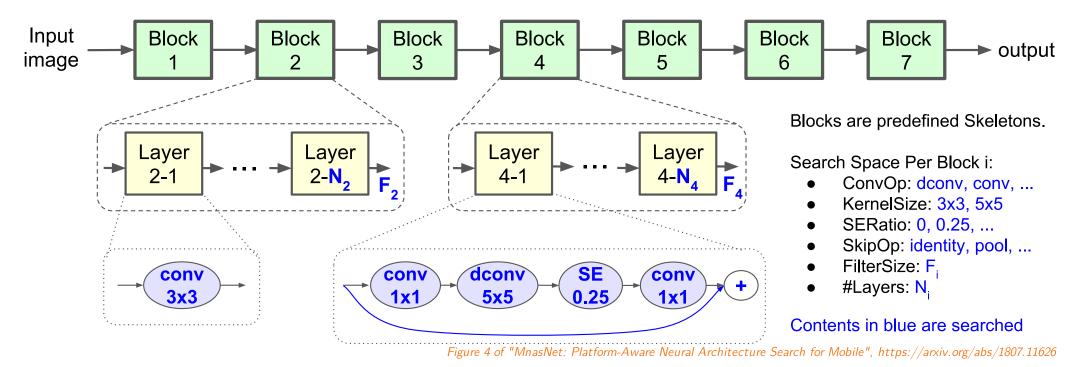
where the constant 0.07 balances the accuracy and FLOPS (the constant comes from an empirical observation that doubling the FLOPS brings about 5% relative accuracy gain, and $1.05 = 2^{\beta}$ gives $\beta \approx 0.0704$).

- It uses a different search space allowing to control kernel sizes and channels in different parts of the architecture (compared to using the same cell everywhere as in NASNet).
- Training directly on ImageNet, but only for 5 epochs.

In total, 8k model architectures are sampled, and PPO algorithm is used instead of the REINFORCE with baseline.

EfficientNet Search





The overall architecture consists of 7 blocks, each described by 6 parameters – 42 parameters in total, compared to 50 parameters of ^{• Convolutional kernel size KernelSize: 3x3, 5x5.} the NASNet search space.

- Convolutional ops *ConvOp*: regular conv (conv), depthwise conv (dconv), and mobile inverted bottleneck conv [29].
- Squeeze-and-excitation [13] ratio SERatio: 0, 0.25.
- Skip ops *SkipOp*: pooling, identity residual, or no skip.
- Output filter size F_i .
- Number of layers per block N_i .

Page 4 of "MnasNet: Platform-Aware Neural Architecture Search for Mobile" https://arxiv.org/abs/1807.11626

RL

NAS Baseline

EfficientNet-B0 Baseline Network



Stage	Operator	Resolution	#Channels	#Layers
i	$\hat{\mathcal{F}}_i$	$\hat{H}_i imes \hat{W}_i$	\hat{C}_i	\hat{L}_i
1	Conv3x3	224×224	32	1
2	MBConv1, k3x3	112×112	16	1
3	MBConv6, k3x3	112×112	24	2
4	MBConv6, k5x5	56 imes 56	40	2
5	MBConv6, k3x3	28 imes 28	80	3
6	MBConv6, k5x5	14×14	112	3
7	MBConv6, k5x5	14×14	192	4
8	MBConv6, k3x3	7 imes 7	320	1
9	Conv1x1 & Pooling & FC	7 imes 7	1280	1

Table 1 of "EfficientNet: Rethinking Model Scaling for Convolutional Neural Networks", https://arxiv.org/abs/1905.11946

RL

MDP

Baseline NAS

What Next



If you liked the introduction to the deep reinforcement learning, I have a whole course **NPFL122 – Deep Reinforcement Learning**.

- It covers a range of reinforcement learning algorithms, from the basic ones to more advanced algorithms utilizing deep neural networks.
- Previously it was in winter semester, but it will be in the summer semester starting from the next year.
- This year it was 2/2 C+Ex, but I want to lengthen it to 3/2 C+Ex, like the Deep learning.
- An elective (povinně volitelný) course in the programs:
 - Artificial Intelligence,

RL

 $\circ~$ Language Technologies and Computational Linguistics.

REINFORCE

Baseline NAS



Generative Models

NPFL114, Lecture 12

MABandits

RL

REINFORCE

MDP

Baseline NAS

RLWhatNext

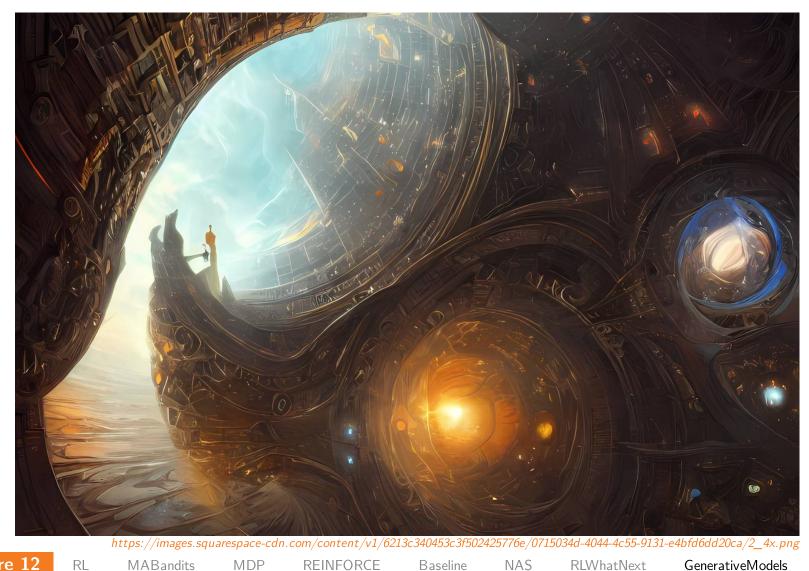
GenerativeModels

36/56

VAE

Generative Models





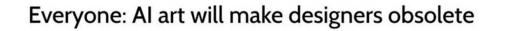
NPFL114, Lecture 12

MABandits MDP REINFORCE Baseline NAS RLWhatNext GenerativeModels VAE

Generative Models

Everyone: AI art will make designers obsolete

Al accepting the job:



Al accepting the job:



RL MDP VAE

NPFL114, Lecture 12

MABandits

REINFORCE

Baseline NAS

RLWhatNext

GenerativeModels



Generative Models

Ú F_AL

Generative models are given a set of realizations of a random variable ${f x}$ and their goal is to estimate $P({f x})$.

Usually the goal is to be able to sample from $P(\mathbf{x})$, but sometimes an explicit calculation of $P(\mathbf{x})$ is also possible.

MDP

Deep Generative Models



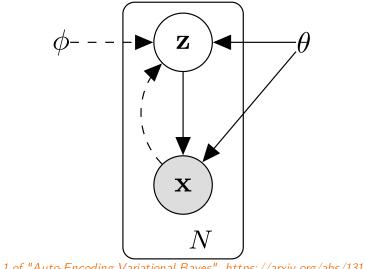


Figure 1 of "Auto-Encoding Variational Bayes", https://arxiv.org/abs/1312.6114

One possible approach to estimate $P(\mathbf{x})$ is to assume that the random variable \mathbf{x} depends on a **latent variable z**:

$$P(oldsymbol{x}) = \sum_{oldsymbol{z}} P(oldsymbol{z}) P(oldsymbol{x} | oldsymbol{z}) = \mathbb{E}_{oldsymbol{z} \sim P(oldsymbol{z})} P(oldsymbol{x} | oldsymbol{z}).$$

We use neural networks to estimate the conditional probability $P_{\theta}(\boldsymbol{x}|\boldsymbol{z})$.

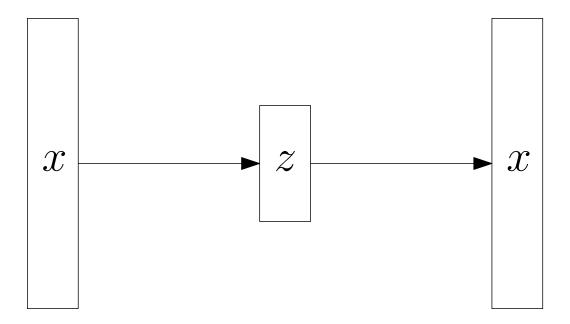
RL

REINFORCE

Baseline NAS

AutoEncoders

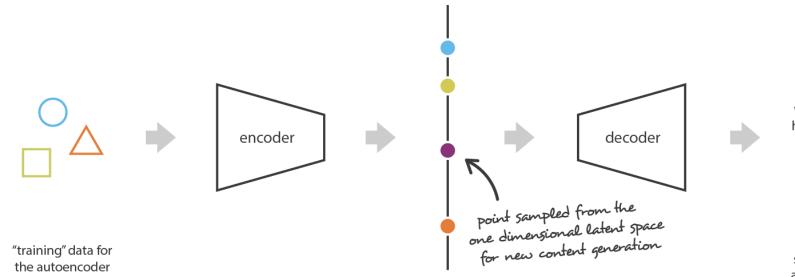




- Autoencoders are useful for unsupervised feature extraction, especially when performing input compression (i.e., when the dimensionality of the latent space z is smaller than the dimensionality of the input).
- When $oldsymbol{x}+oldsymbol{arepsilon}$ is used as input, autoencoders can perform denoising.
- However, the latent space z does not need to be fully covered, so a randomly chosen z does not need to produce a valid x.

AutoEncoders





encoded data can be decoded without loss if the autoencoder has enough degrees of freedom

without explicit regularisation, some points of the latent space

are "meaningless" once decoded

VAE

https://miro.medium.com/max/3608/1*iSfaVxcGi_ELkKgAG0YRlQ@2x.png

NPFL114, Lecture 12

MABandits

RL

REINFORCE

MDP

Baseline NAS

RLWhatNext

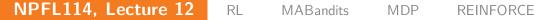
GenerativeModels

Variational AutoEncoders

We assume $P(\mathbf{z})$ is fixed and independent on \mathbf{x} .

We approximate $P(\boldsymbol{x}|\boldsymbol{z})$ using $P_{\boldsymbol{\theta}}(\boldsymbol{x}|\boldsymbol{z})$. However, in order to train an autoencoder, we need to know the posterior $P_{\theta}(\boldsymbol{z}|\boldsymbol{x})$, which is usually intractable.

We therefore approximate $P_{\boldsymbol{\theta}}(\boldsymbol{z}|\boldsymbol{x})$ by a trainable $Q_{\varphi}(\boldsymbol{z}|\boldsymbol{x})$.



Jensen's Inequality

To derive a loss for training variational autoencoders, we first formulate the Jensen's inequality. Recall that convex functions by definition fulfil that for $\boldsymbol{u}, \boldsymbol{v}$ and real $0 \le t \le 1$,

$$f(toldsymbol{u}+(1-t)oldsymbol{v})\leq tf(oldsymbol{u})+(1-t)f(oldsymbol{v}).$$

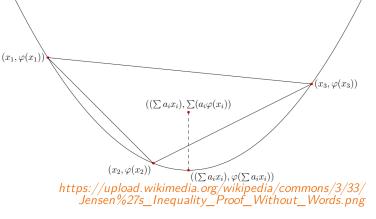
The **Jensen's inequality** generalizes the above property to any *convex* combination of points: if we have $u_i \in \mathbb{R}^D$ and $_{https://upload.wikimedia.org/wikipedia/commons/c/c7/ConvexFunction.svg}$ weights $w_i \in \mathbb{R}^+$ such that $\sum_i w_i = 1$, it holds that

$$fig(\sum_i w_i oldsymbol{u}_iig) \leq \sum_i w_i fig(oldsymbol{u}_iig).$$

The Jensen's inequality can be formulated also for probability distributions (whose expectation can be considered an infinite convex combination):

$$fig(\mathbb{E}[\mathbf{u}]ig) \leq \mathbb{E}_{\mathbf{u}}ig[f(\mathbf{u})ig].$$

d $tf(x_1) + (1-t)f(x_2)$ $f(tx_1 + (1-t)x_2)$ $tx_1 + (1-t)x_2$ $tx_1 + (1-t)x_2$ tx_2 $tx_1 + (1-t)x_2$ tx_2 tx_2 t



MABandits MDP

RL

REINFORCE

Baseline NAS

AS RLWhatNext

GenerativeModels VAE 44/56



VAE – Loss Function Derivation



Our goal will be to maximize the log-likelihood as usual, but we need to express it using the latent variable z:

$$\log P_{oldsymbol{ heta}}(oldsymbol{x}) = \log \mathbb{E}_{P(oldsymbol{z})}ig[P_{oldsymbol{ heta}}(oldsymbol{x}|oldsymbol{z})ig].$$

However, approximating the expectation using a single sample has monstrous variance, because for most z, $P_{\theta}(x|z)$ will be nearly zero.

We therefore turn to our *encoder*, which is able for a given $m{x}$ to generate "its" $m{z}$:

$$egin{aligned} \log P_{m{ heta}}(m{x}) &= \log \mathbb{E}_{P(m{z})}ig[P_{m{ heta}}(m{x}|m{z})ig] \ &= \log \mathbb{E}_{Q_{arphi}(m{z}|m{x})}igg[P_{m{ heta}}(m{x}|m{z})\cdotrac{P(m{z})}{Q_{arphi}(m{z}|m{x})}igg] \ &\geq \mathbb{E}_{Q_{arphi}(m{z}|m{x})}igg[\log P_{m{ heta}}(m{x}|m{z}) + \lograc{P(m{z})}{Q_{arphi}(m{z}|m{x})}igg] \ &= \mathbb{E}_{Q_{arphi}(m{z}|m{x})}igg[\log P_{m{ heta}}(m{x}|m{z})igg] - D_{\mathrm{KL}}igg(Q_{arphi}(m{z}|m{x})\|P(m{z})igg). \end{aligned}$$

NPFL114, Lecture 12

RL

Baseline

VAE – Variational (or Evidence) Lower Bound

The resulting variational lower bound or evidence lower bound (ELBO), denoted $\mathcal{L}(\theta, \varphi; \mathbf{x})$, can be also defined explicitly as:

$$\mathcal{L}(oldsymbol{ heta},oldsymbol{arphi};\mathbf{x}) = \log P_{oldsymbol{ heta}}(oldsymbol{x}) - D_{ ext{KL}}ig(Q_{oldsymbol{arphi}}(oldsymbol{z}|oldsymbol{x})ig\|P_{oldsymbol{ heta}}(oldsymbol{z}|oldsymbol{x})ig).$$

Because KL-divergence is nonnegative, $\mathcal{L}(\boldsymbol{\theta}, \boldsymbol{\varphi}; \mathbf{x}) \leq \log P_{\boldsymbol{\theta}}(\boldsymbol{x}).$

By using simple properties of conditional and joint probability, we get that

$$egin{split} \mathcal{L}(oldsymbol{ heta},oldsymbol{arphi};\mathbf{x}) &= \mathbb{E}_{Q_arphi(oldsymbol{z}|oldsymbol{x})}igg[\log P_{oldsymbol{ heta}}(oldsymbol{x}) + \log P_{oldsymbol{ heta}}(oldsymbol{z}|oldsymbol{x})igg] \ &= \mathbb{E}_{Q_arphi(oldsymbol{z}|oldsymbol{x})}igg[\log P_{oldsymbol{ heta}}(oldsymbol{x},oldsymbol{z}) - \log Q_arphi(oldsymbol{z}|oldsymbol{x})igg] \ &= \mathbb{E}_{Q_arphi(oldsymbol{z}|oldsymbol{x})}igg[\log P_{oldsymbol{ heta}}(oldsymbol{x}|oldsymbol{z}) + \log P(oldsymbol{z}) - \log Q_arphi(oldsymbol{z}|oldsymbol{x})igg] \ &= \mathbb{E}_{Q_arphi(oldsymbol{z}|oldsymbol{x})}igg[\log P_{oldsymbol{ heta}}(oldsymbol{x}|oldsymbol{z}) + \log P(oldsymbol{z}) - \log Q_arphi(oldsymbol{z}|oldsymbol{x})igg] \ &= \mathbb{E}_{Q_arphi(oldsymbol{z}|oldsymbol{x})}igg[\log P_{oldsymbol{ heta}}(oldsymbol{x}|oldsymbol{z})igg] - D_{ ext{KL}}igg(Q_arphi(oldsymbol{z}|oldsymbol{x}))igg]. \end{split}$$

NPFL114, Lecture 12

RL

REINFORCE

Baseline NAS

RLWhatNext

GenerativeModels

VAE



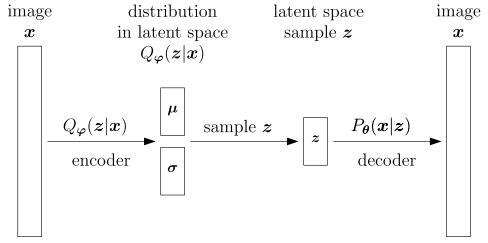
$$-\mathcal{L}(oldsymbol{ heta},oldsymbol{arphi};\mathbf{x}) = \mathbb{E}_{Q_{oldsymbol{arphi}}(oldsymbol{z}|oldsymbol{x})}igg[-\log P_{oldsymbol{ heta}}(oldsymbol{x}|oldsymbol{z})igg] + D_{ ext{KL}}igl(Q_{oldsymbol{arphi}}(oldsymbol{z}|oldsymbol{x})\|P(oldsymbol{z})igr)$$

- We train a VAE by minimizing the $-\mathcal{L}(\boldsymbol{ heta}, \boldsymbol{arphi}; \mathbf{x})$.
- The $\mathbb{E}_{Q_{\varphi}(\boldsymbol{z}|\boldsymbol{x})}$ is estimated using a single sample.
- The distribution $Q_{\varphi}(\boldsymbol{z}|\boldsymbol{x})$ is parametrized as a normal distribution $\mathcal{N}(\boldsymbol{z}|\boldsymbol{\mu}, \boldsymbol{\sigma}^2)$, with the model predicting $\boldsymbol{\mu}$ and $\boldsymbol{\sigma}$ given \boldsymbol{x} .
 - In order for σ to be positive, we can use exp activation function (so that the network predicts $\log \sigma$ before the activation), or for example a softplus activation function.
 - $^{\circ}$ The normal distribution is used, because we can sample from it efficiently, we can backpropagate through it and we can compute D_{KL} analytically; furthermore, if we decide to parametrize $Q_{\varphi}(\boldsymbol{z}|\boldsymbol{x})$ using mean and variance, the maximum entropy principle suggests we should use the normal distribution.
- We use a prior $P(\boldsymbol{z}) = \mathcal{N}(\boldsymbol{0}, \boldsymbol{I}).$

Variational AutoEncoders Training



$$-\mathcal{L}(oldsymbol{ heta},oldsymbol{arphi};\mathbf{x}) = \mathbb{E}_{Q_{oldsymbol{arphi}}(oldsymbol{z}|oldsymbol{x})}igg[-\log P_{oldsymbol{ heta}}(oldsymbol{x}|oldsymbol{z})igg] + D_{ ext{KL}}igl(Q_{oldsymbol{arphi}}(oldsymbol{z}|oldsymbol{x})\|P(oldsymbol{z})igr)$$



Note that the loss has 2 intuitive components:

- reconstruction loss starting with x, passing though Q_{φ} , sampling z and then passing through P_{θ} should arrive back at x;
- latent loss over all *x*, the distribution of Q_φ(*z*|*x*) should be as close as possible to the prior P(*z*) = N(0, *I*), which is independent on *x*.

Variational AutoEncoders – Reparametrization Trick



In order to backpropagate through $m{z} \sim Q_{m{arphi}}(m{z}|m{x})$, note that if

 $oldsymbol{z} \sim \mathcal{N}(oldsymbol{\mu}, oldsymbol{\sigma}^2),$

we can write \boldsymbol{z} as

$$oldsymbol{z} \sim oldsymbol{\mu} + oldsymbol{\sigma} \odot \mathcal{N}(oldsymbol{0},oldsymbol{I}).$$

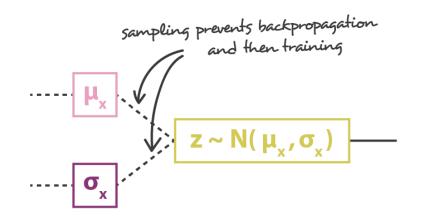
Such formulation then allows differentiating z with respect to μ and σ and is called a **reparametrization trick** (Kingma and Welling, 2013).

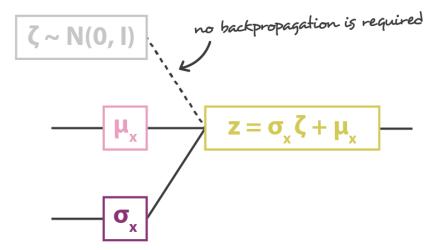


Variational AutoEncoders – Reparametrization Trick

no problem for backpropagation

---- backpropagation is not possible due to sampling





sampling without reparametrisation trick

sampling with reparametrisation trick

https://miro.medium.com/max/3704/1*S8CoO3TGtFBpzv8GvmgKeg@2x.png

NPFL114, Lecture 12

MABandits

RL

MDP REINFORCE

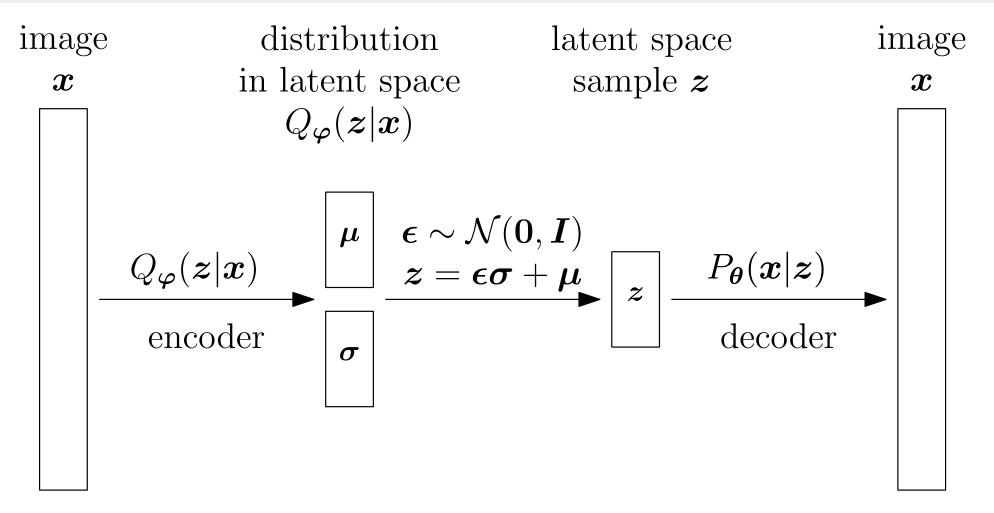
Baseline

NAS RLW

RLWhatNext Gen

GenerativeModels VAE 50/56

Variational AutoEncoders – Reparametrization Trick



NPFL114, Lecture 12

MDP

RL

REINFORCE

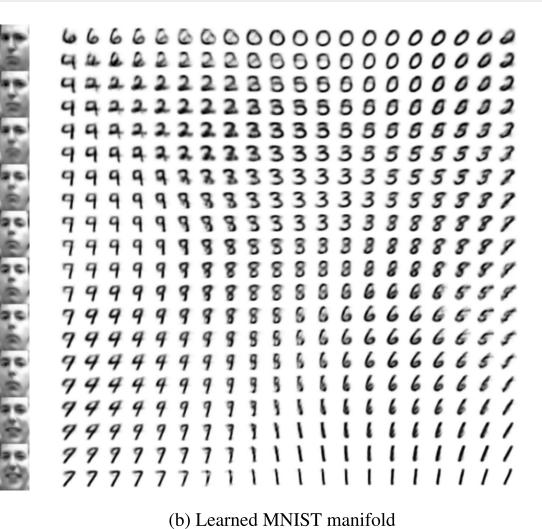
Baseline NAS

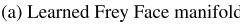
GenerativeModels

VAE

Variational AutoEncoders







RL

(a) Learned Frey Face manifold

Figure 4 of "Auto-Encoding Variational Bayes", https://arxiv.org/abs/1312.6114

NPFL114, Lecture 12

MDP

REINFORCE

Baseline

NAS RLWhatNext GenerativeModels

VAE



2 + 20431950

(a) 2-D latent space

(b) 5-D latent space

MDP

(c) 10-D latent space (d) 20-D latent space Figure 5 of "Auto-Encoding Variational Bayes", https://arxiv.org/abs/1312.6114

NPFL114, Lecture 12

MABandits

RL

REINFORCE

Baseline NAS

RLWhatNext

GenerativeModels

53/56

VAE

Variational AutoEncoders





NPFL114, Lecture 12

MABandits

RL

MDP REINFORCE

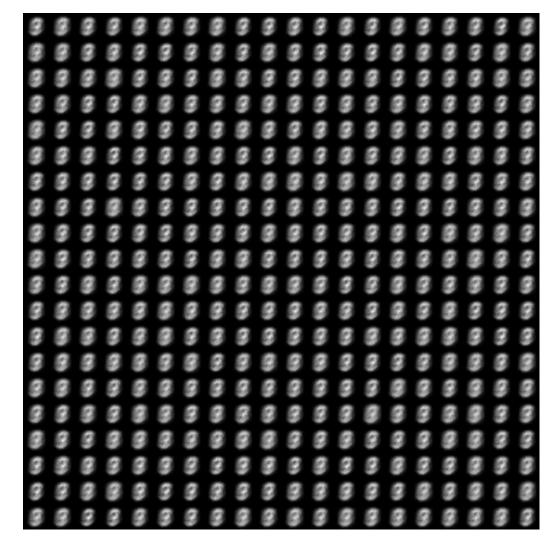
Baseline

NAS

RLWhatNext

GenerativeModels VAE

Variational AutoEncoders – Too High Latent Loss



NPFL114, Lecture 12

RL



Variational AutoEncoders – Too High Reconstruction Loss



	10	\mathcal{G}	De:	5.	3	100	1.	1	10	1	64	3	$\mathcal{F}_{\mathcal{F}}$	Ċ		\$	1.2	ħ.	E	19
10	Į,	12:	19	3	63	E.	\mathcal{G}_{i}	\mathbf{z}	$\mathcal{D}_{\mathcal{C}}$	9	3	đ	2		Ø	4	3	19	69	2
64.		Ľ	5		0.0	1	<u>G</u>	B	3	Ë	2	4	5	3	N.	\mathcal{G}	121	n	9	3
2	Ź	E.	6	N)	14	3	ŝ	Ģ	\mathcal{T}	$\{i\}$	3	ş	30	Ċ,	64	T.	3	C St	$\boldsymbol{\mu}$	17
1	Č,	1.14	4	8	4	2.2	53	1	G	4	$\mathbb{C}^{(i)}$	10	3	E	10	$\mathcal{L}_{\mathcal{O}}$	3	1.	K	đ.
19		ŝą	3	93	14	$\mathbf{c}_{\mathbf{b}}$	14	10		\mathbf{S}_{i}	3	3	13	5	\mathcal{L}_{i}	$\mathcal{S}_{\mathcal{S}}$		10	4	1
-	ŝ				G^{r}	3	E.		E.	7	3	3	4			17		\mathfrak{O}	Ð	\tilde{L}_{n}
5	1-	${\mathbb C}^{n}$	N	1	2		5	7	2	್ಷ	52	R			ą.	Æ	3	3	4	E_{0}
1		3	13		22	3				3	ŝ	\$	1	18	4	50	2		5	1
1		ie à	23	φ^*	1	3	\mathcal{L}	0. 16	\tilde{X}	10	Q_{i}			42	157	14	12			\hat{c}
Ç		1	3	(C)	X	6R	1	3	5	14	13	4	\tilde{G}_{i}^{i}	3	1	Λ_{C}^{α}	3		9	1.2
1		64	X	6	2	d.	3	$\langle \hat{\boldsymbol{\omega}} \rangle$	4	51	15	15	3	3	3	$\langle z \rangle$	47		18	S.
99	2	1	1	3	10	\hat{c}	5	12	4	$\mathcal{L}_{\mathcal{O}}$	\mathcal{T}	65	10	g	2	Š	3	E.	5.	6
	Î	5	10	${\mathcal C}_{i}$	1	S	÷.		1		C.	X	3	2	G.	1	2	4	6	2
54		ŝ	3	1	15		\mathcal{R}	i S	5	\mathbb{S}^{3}	\$	3	÷.	3	3	Ø	PH	\mathcal{L}	1	S.
6	7	3	5	6	Ċ	Col-		1	2	ŝ	δ_{Q}^{*}	4	$\{ z \}_{i \in I}$	225	100	35	2	(0)	18.	No.
2	5	0	1.4	di.	1	24	15	6	2	$\mathcal{O}_{\mathcal{O}}$	Ť	\mathcal{F}	\mathfrak{S}	30	40	8	\mathbb{Z}_{2}^{n}	3	$\tilde{\mathcal{D}}$	63
2	ġ	5	3	2		2	<i>§</i> .	7	3	3	2	8	Sec.	¥	10	£3)	30	\$	4	3
ť.	ş	3	3	3	3	5.	D	4	4	3	5	14	3	3	3	$\widehat{\mathcal{O}}_{\mathcal{O}}^{1}$	1	$(\mathbf{\bar{r}})$	ð	ç,
2	2	10	41	12	17	2	R	4	10	1	245	6	5	Paris -		S.	\$	\mathcal{X}_{i}	8	5

NPFL114, Lecture 12

RL

Baseline NAS

RLWhatNext

GenerativeModels

VAE