NPFL114, Lecture 3



Training Neural Networks II

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unless otherwise stated



Let us have a dataset with training, validation and test sets, each containing examples (x, y). Depending on y, consider one of the following output activation functions:

none	$\text{ if }y\in \mathbb{R},$
σ	if y is a probability of an outcome,
$\operatorname{softmax}$	if y is a gold class index out of K classes (or a full distribution).

If $\boldsymbol{x} \in \mathbb{R}^D$, we can use a neural network with an input layer of size D, hidden layer of size H with a non-linear activation function, and an output layer of size O (either 1 or number of classification classes) with the mentioned output function.

BTW, there are of course many functions, which could be used as output activations instead of σ and softmax; however, σ and softmax are almost universally used. One of the reason is that they can be derived using the maximum-entropy principle from a set of conditions, see the <u>Machine Learning for Greenhorns (NPFL129) lecture 5 slides</u>. Additionally, they are the inverses of canonical link functions of the Bernoulli and categorical distributions, respectively.

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Convergence



We have

$$oldsymbol{h}_i = f^{(1)}\left(\sum_j oldsymbol{W}_{i,j}^{(1)}oldsymbol{x}_j + oldsymbol{b}_i^{(1)}
ight)$$

where

- $\boldsymbol{W}^{(1)} \in \mathbb{R}^{H imes D}$ is a matrix of *weights*,
- $oldsymbol{b}^{(1)} \in \mathbb{R}^H$ is a vector of *biases*,
- $f^{(1)}$ is an activation function.

Dropout

The weights are sometimes also called a *kernel*.

The biases define general behaviour in case of zero/very small input.

Transformations of type $\boldsymbol{w}^T \boldsymbol{x} + b$ are called *affine* instead of *linear*.

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NNTraining Metrics&Losses



Similarly

 $oldsymbol{o}_i = f^{(2)}\left(\sum_j oldsymbol{W}_{i,j}^{(2)}oldsymbol{h}_j + oldsymbol{b}_i^{(2)}
ight)$

with

- $\boldsymbol{W}^{(2)} \in \mathbb{R}^{O \times H}$ another matrix of weights,
- $oldsymbol{b}^{(2)} \in \mathbb{R}^O$ another vector of biases,
- $f^{(2)}$ being an output activation function.

Dropout

The parameters of the model are therefore $m{W}^{(1)}, m{W}^{(2)}, m{b}^{(1)}, m{b}^{(2)}$ of total size D imes H + H imes O + H + O.

To train the network, we repeatedly sample m training examples and perform SGD (or any of its adaptive variants), updating the parameters to minimize the loss.

$$oldsymbol{ heta}_i \leftarrow oldsymbol{ heta}_i - lpha rac{\partial L}{\partial oldsymbol{ heta}_i}$$

We set the hyperparameters (size of the hidden layer, hidden layer activation function, learning rate, ...) using performance on the validation set and evaluate generalization error on the test set.

Practical Issues

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- Processing all data in *batches*.
- Vector representation of the network.

Instead of $m{h}_i = f^{(1)}\left(\sum_j m{W}^{(1)}_{i,j}m{x}_j + m{b}^{(1)}_i
ight)$, we usually write

$$oldsymbol{h} = f^{(1)}\left(oldsymbol{W}^{(1)}oldsymbol{x} + oldsymbol{b}^{(1)}
ight)$$

$$m{o} = f^{(2)} \left(m{W}^{(2)} m{h} + m{b}^{(2)}
ight) = f^{(2)} \left(m{W}^{(2)} \left(f^{(1)} \left(m{W}^{(1)} m{x} + m{b}^{(1)}
ight)
ight) + m{b}^{(2)}
ight)$$

The derivatives

$$rac{\partial f^{(1)}\left(oldsymbol{W}^{(1)}oldsymbol{x}+oldsymbol{b}^{(1)}
ight)}{\partialoldsymbol{x}},rac{\partial f^{(1)}\left(oldsymbol{W}^{(1)}oldsymbol{x}+oldsymbol{b}^{(1)}
ight)}{\partialoldsymbol{W}^{(1)}}$$

are then matrices (called *Jacobians*) or even higher-dimensional tensors.

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Regularization Dropout

LabelSmoothing

Computation Graph





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High Level Overview



	Classical ('90s)	Deep Learning
Architecture	• • • • • • • • •	::::::::::::::::::::::::::::::::::::::
Activation func.	$ anh, \sigma$	anh, ReLU, PReLU, ELU, GELU, Swish, Mish,
Output function	none, σ	none, σ , softmax
Loss function	MSE	NLL (or cross-entropy or KL-divergence)
Optimization	SGD, momentum	SGD (+ momentum), RMSProp, Adam, SGDW, AdamW,
Regularization	L2, L1	L2, Dropout, Label smoothing, BatchNorm, LayerNorm, Mi×Up, WeightStandardization,

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Metrics and Losses



During training and evaluation, we use two kinds of error functions:

- **loss** is a *differentiable* function used during training,
 NLL, MSE, Huber loss, Hinge, ...
- metric is any (and very often non-differentiable) function used during evaluation,
 o any loss, accuracy, F-score, BLEU, ...
 - $^{\circ}\,$ possibly even human evaluation.

In TensorFlow, the losses and metrics are available in tf.losses and tf.metrics (aliases for tf.keras.losses and tf.keras.metrics).

TF Losses



The tf.losses offer two sets of APIs. The current ones are loss classes like

```
tf.losses.MeanSquaredError(
    reduction=tf.losses.Reduction.AUTO, name='mean_squared_error'
)
```

The created objects are subclasses of tf.losses.Loss and can be always called with three arguments:

```
__call__(y_true, y_pred, sample_weight=None)
```

which returns the loss of the given data, *reduced* using the specified reduction. If <code>sample_weight</code> is given, it is used to weight (multiply) the individual batch examples before reduction.

- tf.losses.Reduction.SUM_OVER_BATCH_SIZE, which is the default of .AUTO;
- tf.losses.Reduction.SUM;
- tf.losses.Reduction.NONE.

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TF Cross-entropy Losses



The cross-entropy losses need to specify also the distribution in question:

- tf.losses.BinaryCrossentropy: the gold and predicted distributions are Bernoulli distributions (i.e., a single probability);
- tf.losses.CategoricalCrossentropy: the gold and predicted distributions are categorical distributions;
- tf.losses.SparseCategoricalCrossentropy: a special case, where the gold distribution is one-hot distribution (i.e., a single correct class), which is represented as the gold *class index*; therefore, it has one less dimension than the predicted distribution.

These losses expect probabilities on input, but offer from_logits argument, which can be used to indicate that logits are used instead of probabilities.

Old losses API

In addition to the loss objects, tf.losses offers methods like tf.losses.mean_squared_error, which process two arguments y_true and y_pred.

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TF Metrics



There are two important differences between metrics and losses.

- 1. metrics may be non-differentiable;
- 2. metrics aggregate results over multiple batches.

The metric objects are subclasses of tf.losses.Metric and offer the following method:

- update_state(y_true, y_pred, sample_weight=None) updates the value of the metric and stores it;
- result() returns the current value of the metric;
- reset_states() clears the stored state of the metric.

The most common pattern is using the provided

__call__(y_true, y_pred, sample_weight=None)

method, which is a combination of update_state followed by a result().

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TF Metrics



Apart from analogues of the losses

- tf.metrics.MeanSquaredError
- tf.metrics.BinaryCrossentropy
- tf.metrics.CategoricalCrossentropy
- tf.metrics.SparseCategoricalCrossentropy

the tf.metrics provide

- tf.metrics.Mean computes averaged mean;
- tf.metrics.Accuracy returns accuracy, which is an average number of examples where the prediction is equal to the gold value;
- tf.metrics.BinaryAccuracy returns accuracy of predicting a Bernoulli distribution (the gold value is 0/1, the prediction is a probability);
- tf.metrics.CategoricalAccuracy returns accuracy of predicting a Categorical distribution (the argmaxes of gold and predicted distributions are equal);
- tf.metrics.SparseCategoricalAccuracy again a special case, there the gold distribution is represented as the gold *class index*.

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Derivative of MSE Loss



Given the MSE loss of

$$L = ig(y - \hat{y}(oldsymbol{x};oldsymbol{ heta})ig)^2 = ig(\hat{y}(oldsymbol{x};oldsymbol{ heta}) - yig)^2,$$

the derivative with respect to \hat{y} is simply:

$$rac{\partial L}{\hat{y}(oldsymbol{x};oldsymbol{ heta})} = 2ig(\hat{y}(oldsymbol{x};oldsymbol{ heta}) - yig).$$

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Softmax



Let us have a softmax output layer with

$$oldsymbol{p}_i = rac{e^{oldsymbol{z}_i}}{\sum_j e^{oldsymbol{z}_j}}.$$

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Consider now the MLE estimation. The loss for gold class index *gold* is then

$$L(ext{softmax}(oldsymbol{z}), ext{gold}) = -\logoldsymbol{o}_{gold}.$$

The derivation of the loss with respect to \boldsymbol{z} is then

$$egin{aligned} rac{\partial L}{\partial oldsymbol{z}_i} &= rac{\partial}{\partial oldsymbol{z}_i} \left[-\log rac{e^{oldsymbol{z}_{gold}}}{\sum_j e^{oldsymbol{z}_j}}
ight] = - rac{\partial oldsymbol{z}_{gold}}{\partial oldsymbol{z}_i} + rac{\partial \log(\sum_j e^{oldsymbol{z}_j})}{\partial oldsymbol{z}_i} \ &= - \left[gold = i
ight] + rac{1}{\sum_j e^{oldsymbol{z}_j}} e^{oldsymbol{z}_i} \ &= - \left[gold = i
ight] + oldsymbol{o}_i. \end{aligned}$$

Therefore, $\frac{\partial L}{\partial z} = o - \mathbf{1}_{gold}$, where $\mathbf{1}_{gold}$ is 1 at index gold and 0 otherwise.

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Derivative of Softmax and Sigmoid MLE Losses

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In the previous case, the gold distribution was *sparse*, with only one target probability being 1. In the case of general gold distribution \boldsymbol{g} , we have

$$L(ext{softmax}(oldsymbol{z}),oldsymbol{g}) = -\sum_i oldsymbol{g}_i \log oldsymbol{o}_i.$$

Repeating the previous procedure for each target probability, we obtain

$$rac{\partial L}{\partial oldsymbol{z}} = oldsymbol{o} - oldsymbol{g}.$$

Sigmoid

Analogously, for $o = \sigma(z)$ we get $rac{\partial L}{\partial z} = o - g$, where g is the target gold probability.

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Regularization



As already mentioned, regularization is any change in the machine learning algorithm that is designed to reduce generalization error but not necessarily its training error.

Regularization is usually needed only if training error and generalization error are different. That is often not the case if we process each training example only once. Generally the more training data, the better generalization performance.

- Early stopping
- L2, L1 regularization
- Dataset augmentation
- Ensembling
- Dropout
- Label smoothing

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Regularization – Early Stopping



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L2 Regularization



We prefer models with parameters small under L2 metric.

The L2 regularization, also called *weight decay*, *Tikhonov regularization* or *ridge regression* therefore minimizes

$$ilde{J}(oldsymbol{ heta};\mathbb{X})=J(oldsymbol{ heta};\mathbb{X})+\lambda\|oldsymbol{ heta}\|_2^2$$

for a suitable (usually very small) λ .

During the parameter update of SGD, we get

$$oldsymbol{ heta}_i \leftarrow oldsymbol{ heta}_i - lpha rac{\partial J}{\partial oldsymbol{ heta}_i} - 2lpha \lambda oldsymbol{ heta}_i$$

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L2 Regularization





Figure 7.1, page 233 of Deep Learning Book, http://deeplearningbook.org

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L2 Regularization as MAP

Another way to arrive at L2 regularization is to utilize Bayesian inference. With MLE we have

$$oldsymbol{ heta}_{ ext{MLE}} = rg\max_{oldsymbol{ heta}} p(\mathbb{X};oldsymbol{ heta}).$$

Instead, we may want to maximize *maximum a posteriori (MAP)* point estimate:

$$oldsymbol{ heta}_{ ext{MAP}} = rg\max_{oldsymbol{ heta}} p(oldsymbol{ heta}; \mathbb{X})$$

Using Bayes' theorem

$$p(oldsymbol{ heta};\mathbb{X})=p(\mathbb{X};oldsymbol{ heta})p(oldsymbol{ heta})/p(\mathbb{X}),$$

we get



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L2 Regularization as MAP

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The $p(\boldsymbol{\theta})$ are prior probabilities of the parameter values (our *preference*).

One possibility for such a prior is $\mathcal{N}(\boldsymbol{\theta}; 0, \sigma^2)$, which corresponds to *small weights preference*. Then

$$egin{aligned} m{ heta}_{ ext{MAP}} &= rg\max_{m{ heta}} p(\mathbb{X};m{ heta}) p(m{ heta}) \ &= rg\max_{m{ heta}} \prod_{i=1}^m p(m{x}^{(i)};m{ heta}) p(m{ heta}) \ &= rg\min_{m{ heta}} \sum_{i=1}^m -\log p(m{x}^{(i)};m{ heta}) -\log p(m{ heta}) \end{aligned}$$

By substituting the probability of the Gaussian prior, we get

$$oldsymbol{ heta}_{ ext{MAP}} = rgmin_{oldsymbol{ heta}} \sum_{i=1}^m -\log p(oldsymbol{x}^{(i)};oldsymbol{ heta}) - rac{1}{2}\log(2\pi\sigma^2) + rac{\|oldsymbol{ heta}\|_2^2}{2\sigma^2}$$

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L1 Regularization



Similar to L2 regularization, but we prefer low L1 metric of parameters. We therefore minimize

$$ilde{J}(oldsymbol{ heta};\mathbb{X}) = J(oldsymbol{ heta};\mathbb{X}) + \lambda \|oldsymbol{ heta}\|_1$$

The corresponding SGD update is then

$$oldsymbol{ heta}_i \leftarrow oldsymbol{ heta}_i - lpha rac{\partial J}{\partial oldsymbol{ heta}_i} - ext{sign}(oldsymbol{ heta}_i) lpha \lambda.$$

Regularization

Dropout

Regularization – Dataset Augmentation

For some data, it is cheap to generate slightly modified examples.

Image processing: translations, horizontal flips, scaling, rotations, color adjustments, ...
 Mixup (appeared in 2017)



(b) Effect of *mixup* on a toy problem.

Figure 1b of paper "mixup: Beyond Empirical Risk Minimization", https://arxiv.org/abs/1710.09412

- Speech recognition: noise, frequency change, ...
- More difficult for discrete domains like text.

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Regularization – Ensembling

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Ensembling (also called *model averaging* or in some contexts *bagging*) is a general technique for reducing generalization error by combining several models. The models are usually combined by averaging their outputs (either distributions or output values in case of a regression).

The main idea behind ensembling it that if models have uncorrelated (independent) errors, then by averaging model outputs the errors will cancel out. If we denote the prediction of a model y_i on a training example (\boldsymbol{x}, y) as $y_i(\boldsymbol{x}) = y + \varepsilon_i(\boldsymbol{x})$, so that $\varepsilon_i(\boldsymbol{x})$ is the model error on example \boldsymbol{x} , the mean square error of the model is $\mathbb{E}[(y_i(\boldsymbol{x}) - t)^2] = \mathbb{E}[\varepsilon_i^2(\boldsymbol{x})]$.

Because for uncorrelated identically distributed random values \mathbf{x}_i we have

$$\mathrm{Var}\left(\sum \mathrm{x}_i
ight) = \sum \mathrm{Var}(\mathrm{x}_i), \mathrm{Var}(a\cdot \mathrm{x}) = a^2\,\mathrm{Var}(\mathrm{x}),$$

we get that $\operatorname{Var}\left(\frac{1}{n}\sum \varepsilon_i\right) = \frac{1}{n}\cdot\sum \frac{1}{n}\operatorname{Var}(\varepsilon_i)$, so the errors should decrease with the increasing number of models.

However, ensembling usually has high performance requirements.

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Regularization – Ensembling

There are many possibilities how to train the models to average:

• Generate different datasets by sampling with replacement (bagging).



Figure 7.5, page 257 of Deep Learning Book, http://deeplearningbook.org

- Use random different initialization.
- Average models from last hours/days of training.

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Regularization – Dropout

How to design good universal features?

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• In reproduction, evolution is achieved using gene swapping. The genes must not be just good with combination with other genes, they need to be universally good.

Idea of *dropout* by (Srivastava et al., 2014), in preprint since 2012.

When applying dropout to a layer, we drop each neuron independently with a probability of p (usually called *dropout rate*). To the rest of the network, the dropped neurons have value of zero.



(a) Standard Neural Network

Figure 4 of paper "Multiple Instance Fuzzy Inference Neural Networks" by Amine B. Khalifa et al.

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(b) Network after Dropout

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Regularization – Dropout

Dropout is performed only when training, during inference no nodes are dropped. However, in that case we need to *scale the activations down* by a factor of 1 - p to account for more neurons than usual.



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Alternatively, we might scale the activations up during training by a factor of 1/(1-p).



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Regularization – Dropout as Ensembling





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(a) Without dropout

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(b) Dropout with p = 0.5.

Figure 7: Features learned on MNIST with one hidden layer autoencoders having 256 rectified linear units. Figure 7 of paper "Dropout: A Simple Way to Prevent Neural Networks from Overfitting", http://jmlr.org/papers/volume15/srivastava14a/srivastava14a.pdf

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Regularization – Dropout Implementation

```
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```

```
def dropout(inputs, rate=0.5, training=False):
    def do_inference():
        return inputs
```

```
def do_train():
```

```
random_noise = tf.random.uniform(tf.shape(inputs))
mask = tf.cast(tf.less(random_noise, rate), tf.float32)
return inputs * mask / (1 - rate)
```

```
if training:
    return do_train()
else:
    return do_inference()
```

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Regularization – Label Smoothing

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Problem with softmax MLE loss is that it is *never satisfied*, always pushing the gold label probability higher (but it saturates near 1).

This behaviour can be responsible for overfitting, because the network is always commanded to respond more strongly to the training examples, not respecting similarity of different training examples.

Ideally, we would like a full (non-sparse) categorical distribution of classes for training examples, but that is usually not available.

We can at least use a simple smoothing technique, called *label smoothing*, which allocates some small probability volume α uniformly for all possible classes.

The target distribution is then

$$(1-lpha) {f 1}_{gold} + lpha {f 1\over ext{number of classes}}.$$

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Regularization – Label Smoothing





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Regularization – Good Defaults

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When you need to regularize (your model is overfitting), then a good default strategy is to:

- use data augmentation if possible;
- use dropout on all hidden dense layers (not on the output layer), good default dropout rate is 0.5 (or use 0.3 if the model is underfitting);
- use L2 regularization for your convolutional networks;
- use label smoothing (start with 0.1);
- if you require best performance and have a lot of resources, also perform ensembling.

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The training process might or might not converge. Even if it does, it might converge slowly or quickly.

A major issue of convergence of deep networks is to make sure that the gradient with respect to all parameters is reasonable at all times, i.e., it does not decrease or increase too much with depth or in different batches.

There are *many* factors influencing the gradient, convergence and its speed, we now mention three of them:

- saturating non-linearities,
- parameter initialization strategies,
- gradient clipping.

Convergence – Saturating Non-linearities



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Convergence – Parameter Initialization

Neural networks usually need random initialization to break symmetry.

- Biases are usually initialized to a constant value, usually 0.
- Weights are usually initialized to small random values, either with uniform or normal distribution.
 - $\circ~$ The scale matters for deep networks!
 - $\,\circ\,$ Originally, people used $U\left[-\frac{1}{\sqrt{n}},\frac{1}{\sqrt{n}}\right]$ distribution.
 - Xavier Glorot and Yoshua Bengio, 2010: Understanding the difficulty of training deep feedforward neural networks.

The authors theoretically and experimentally show that a suitable way to initialize a $\mathbb{R}^{n\times m}$ matrix is

$$U\left[-\sqrt{rac{6}{m+n}},\sqrt{rac{6}{m+n}}
ight]$$

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Regularization Dropout

Convergence – **Parameter Initialization**





Figure 6 of paper "Understanding the difficulty of training deep feedforward neural networks", http://proceedings.mlr.press/v9/glorot10a/glorot10a.pdf.

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Convergence – **Parameter Initialization**





Figure 7 of paper "Understanding the difficulty of training deep feedforward neural networks", http://proceedings.mlr.press/v9/glorot10a/glorot10a.pdf.

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Convergence – Gradient Clipping





Figure 8.3, page 289 of Deep Learning Book, http://deeplearningbook.org

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Convergence – Gradient Clipping



Figure 10.17, page 414 of Deep Learning Book, http://deeplearningbook.org

Using a given maximum norm, we may *clip* the gradient.

$$oldsymbol{g} \leftarrow egin{cases} oldsymbol{g} & ext{ if } \|oldsymbol{g}\| \leq c, \ c rac{oldsymbol{g}}{\|oldsymbol{g}\|} & ext{ if } \|oldsymbol{g}\| > c. \end{cases}$$

Clipping can be performed per weight (parameter clipvalue of tf.optimizers.Optimizer), per variable (clipnorm) or for the gradient as a whole (global clipnorm). NPFL114, Lecture 3 NNTraining Metrics&Losses & Convergence Convergence