

Haskell and Domain-Specific Languages

Haskell nejen pro informatiky

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<https://wiki.ufal.ms.mff.cuni.cz/courses:pfl080>

Part I

Monad Laws

Functor Laws

```
class Functor f where
```

```
  fmap :: (a -> b) -> (f a -> f b)
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fmap (f . g) ≡ fmap f . fmap g
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```
fmap f xs ≡ xs >>= return . f
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Functor Laws

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class Functor f where
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fmap id ≡ id
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fmap (f . g) ≡ fmap f . fmap g
```

```
fmap f xs ≡ xs >>= return . f
```

```
instance Functor [] where    fmap = map
```

```
instance Functor Tree where
```

```
  fmap f (Node a t) = Node (f a) (map (fmap f) t)
```

Monad Laws

```
class Monad m where
```

```
  (>>=)      :: m a -> (a -> m b) -> m b
```

```
  (>>)       :: m a -> m b -> m b
```

```
  return   :: a -> m a
```

```
  fail     :: String -> m a
```


Monad Laws

```
class Monad m where
```

```
  (>>=)    :: m a -> (a -> m b) -> m b
```

```
  (>>)     :: m a -> m b -> m b
```

```
  return   :: a -> m a
```

```
  fail     :: String -> m a
```

```
return a >>= k ≡ k a
```

Monad Laws

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class Monad m where
```

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  (>>=)    :: m a -> (a -> m b) -> m b
```

```
  (>>)     :: m a -> m b -> m b
```

```
  return   :: a -> m a
```

```
  fail     :: String -> m a
```

```
return a >>= k ≡ k a
```

```
m >>= return ≡ m
```

Monad Laws

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class Monad m where
```

```
  (>>=)      :: m a -> (a -> m b) -> m b
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  (>>)       :: m a -> m b -> m b
```

```
  return    :: a -> m a
```

```
  fail      :: String -> m a
```

```
return a >>= k ≡ k a
```

```
m >>= return ≡ m
```

```
m >>= (\ x -> h x >>= g) ≡ m >>= h >>= g
```

Monad Laws

```
class Monad m where
```

```
  (>>=)    :: m a -> (a -> m b) -> m b
```

```
  (>>)     :: m a -> m b -> m b
```

```
  return   :: a -> m a
```

```
  fail     :: String -> m a
```

```
return a >>= k ≡ k a
```

```
m >>= return ≡ m
```

```
m >>= (\ x -> h x >>= g) ≡ (m >>= h) >>= g
```

```
instance Monad [] where (>>=) x f      = concat (map f x)
```

```
  return x                      = [x]
```

```
  fail                            = []
```

Monad Laws

```
class Monad m where
```

```
  (>>=)    :: m a -> (a -> m b) -> m b
```

```
  (>>)     :: m a -> m b -> m b
```

```
  return   :: a -> m a
```

```
  fail     :: String -> m a
```

```
return a >>= k ≡ k a
```

```
m >>= return ≡ m
```

```
m >>= (\ x -> h x >>= g) ≡ (m >>= \ x -> h x) >>= g
```

```
instance Monad [] where (>>=) x f      = concat (map f x)
```

```
  return x                          = [x]
```

```
  fail                               = []
```

MonadPlus Laws

```
class Monad m => MonadPlus m where
  mzero  :: m a
  mplus  :: m a -> m a -> m a
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MonadPlus Laws

```
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  mzero  :: m a
  mplus  :: m a -> m a -> m a
```

```
m `mplus` mzero ≡ m
```

MonadPlus Laws

```
class Monad m => MonadPlus m where
  mzero  :: m a
  mplus  :: m a -> m a -> m a
```

```
m `mplus` mzero  ≡ m
```

```
mzero `mplus` m  ≡ m
```


MonadPlus Laws

```
class Monad m => MonadPlus m where
  mzero  :: m a
  mplus  :: m a -> m a -> m a
```

```
m `mplus` mzero  ≡ m      m >>= \ _ -> mzero  ≡ mzero
mzero `mplus` m  ≡ m
```

MonadPlus Laws

```
class Monad m => MonadPlus m where
  mzero  :: m a
  mplus  :: m a -> m a -> m a
```

```
m `mplus` mzero  ≡ m      m >>= const mzero  ≡ mzero
mzero `mplus` m  ≡ m      mzero >>= k      ≡ mzero
```

MonadPlus Laws

```
class Monad m => MonadPlus m where
  mzero  :: m a
  mplus  :: m a -> m a -> m a
```

```
m `mplus` mzero  ≡ m      m >>= const mzero  ≡ mzero
mzero `mplus` m  ≡ m      mzero >>= k        ≡ mzero
```

```
instance MonadPlus [] where
  mzero  = []
  mplus  = (++)
```

MonadPlus Laws

```
class Monad m => MonadPlus m where
  mzero  :: m a
  mplus  :: m a -> m a -> m a
```

```
m `mplus` mzero  ≡ m      m >>= const mzero  ≡ mzero
mzero `mplus` m  ≡ m      mzero >>= k       ≡ mzero
```

```
instance MonadPlus [] where mzero = []
                          mplus  = (++)
```

The `IO` monad is **not** an instance of the `MonadPlus` class, since it has no `mzero` that would satisfy the `m >>= const mzero` law (1).

Exercises

Formulate the monad laws using the **do** notation. Discuss any **analogies** with the notations used in **imperative languages**.

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Relate function **application** $f (g x)$ to monadic **binding** $g x \gg= f$ using for instance the **Maybe** instance (1).

Exercises

Formulate the monad laws using the **do** notation. Discuss any analogies with the notations used in **imperative languages**.

Relate function application $f (g x)$ to monadic binding $g x \gg= f$ using for instance the **Maybe** instance (1).

```
instance Monad Maybe where
    Just x  >>= k  = k x
    Nothing >>= k  = Nothing
    return          = Just
    fail s          = Nothing
```

```
instance MonadPlus Maybe where
    mzero = Nothing
    Nothing `mplus` ys = ys
    xs      `mplus` ys = xs
```

Exercises

Formulate the monad laws using the **do** notation. Discuss any analogies with the notations used in **imperative languages**.

Relate function application $f \ \$ \ g \ x$ to monadic binding $f \ =\<< \ g \ x$ using for instance the **Maybe** instance (1).

```
instance Monad Maybe where
  Just x  >>= k = k x
  Nothing >>= k = Nothing
  return  = Just
  fail s  = Nothing
```

```
instance MonadPlus Maybe where
  mzero = Nothing
  Nothing `mplus` ys = ys
  xs      `mplus` ys = xs
```


Part II

Input/Output

The Pure World

```
module Main where
```

```
main :: IO ()
```

```
main = return ()
```

The Pure World

```
module Main where
```

```
main :: IO ()
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main = return ()
```

```
interact :: (String -> String) -> IO ()
```

```
interact f = getContents >>= putStr . f
```

The Pure World

```
module Main where
```

```
main :: IO ()
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```
main = return ()
```

```
interact :: (String -> String) -> IO ()
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```
interact f = getContents >>= putStr . f
```

```
print :: Show a => a -> IO ()
```

```
print = putStrLn . show
```

The Pure World

```
module Main where
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```
main :: IO ()
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main = return ()
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interact :: (String -> String) -> IO ()
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interact f = getContents >>= putStr . f
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```
print :: Show a => a -> IO ()
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```
print = putStrLn . show
```

Explore relevant modules, e.g. `System.IO`, `System.Environment`, `System.Console.GetOpt`, and note the command `:main` in Hugs.



Paul Hudak.

The Haskell School of Expression: Learning Functional Programming through Multimedia.

Cambridge University Press, 2000.