



Dependency Grammars and Treebanks:

Intro – trees, word order, projectivity

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Dependency Grammars and Treebanks (NPFL075)



Lectures: Wednesday, room S1, 15:40-17:10
Markéta Lopatková, Daniel Zeman

Practical sessions:
Jiří Mírovský, Daniel Zeman

<http://ufal.mff.cuni.cz/course/npfl075>

Requirements:

- Homework (40%)
- Activity (10%)
- Final test (50%)

Assessment:

- excellent (= 1) $\geq 90\%$
- very good (= 2) $\geq 70\%$
- good (= 3) $\geq 50\%$

Dependency Grammars and Treebanks



- Family of Prague Dependency Treebanks (PDT, PCEDT)
- Universal Dependencies
- HamleDT, PropBank, ???

Collection of:

- linguistically annotated data
- tools and data format(s)
- documentation

Another point of view:

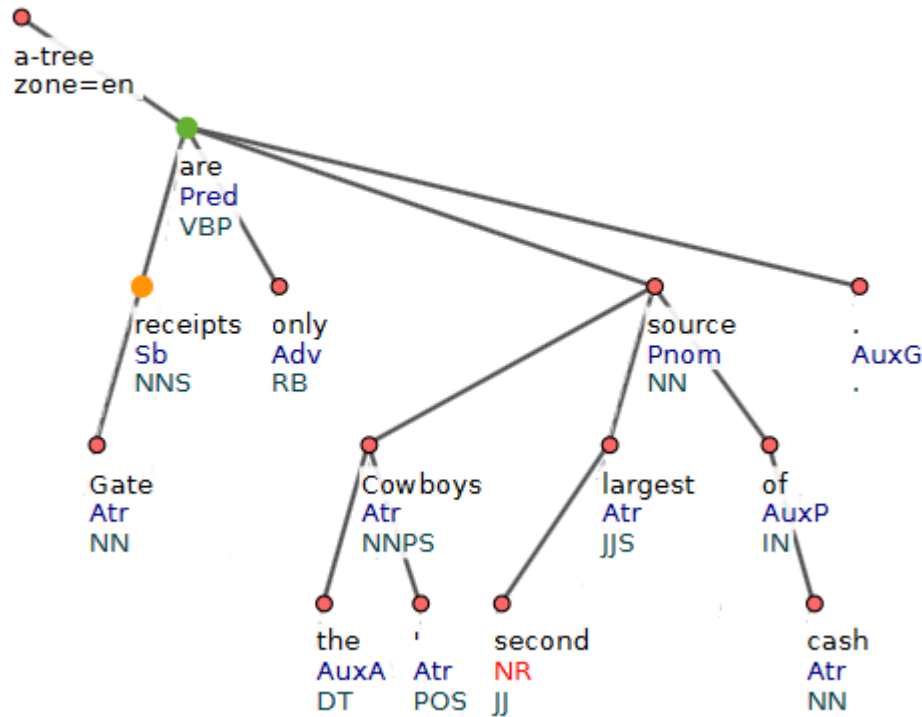
- annotation scheme
- framework for annotation of different languages
- underlying linguistic theory

How to capture sentence structure?



wsj_1411.treex.gz (64/108)

Gate receipts are only the Cowboys' second largest source of cash.



Graph theory: tree



tree (graph theory):

definition:

- finite graph $\langle N, E \rangle$, $N \sim$ nodes/vertices, $E \sim$ edges $\{n_1, n_2\}$
- connected
- no cycles, no loops
- no more than 1 edge between any two different nodes

\Leftrightarrow (undirected) graph

any two nodes are connected by exactly one simple path

rooted tree

- rooted \Rightarrow orientation (i.e., edges ordered pairs $[n_1, n_2]$)

directed tree ... directed graph

- which would be tree
 - if the directions on the edges were ignored, or
 - **all edges are directed towards a particular node** \sim the **root**

Data structure: tree



tree as a data structure:

- rooted tree (as in graph theory)
- all edges are directed from a particular node ~ the **root**

+

- (linear) ordering of nodes:
the children of each node have a specific order

Data structure: tree (properties)



tree as a data structure:

- "tree-ordering" $D \dots$ partial ordering on nodes
 $u \leq v \Leftrightarrow_{\text{def}}$ the unique path from the root to v passes through u
(weak ordering \sim reflexive, antisymmetric, transitive)
- "linear ordering" \dots (partial) ordering on nodes
(strong ordering \sim antireflexive, asymmetric, transitive)

Tree-based structures in CL

two types of tree-based structures in CL:

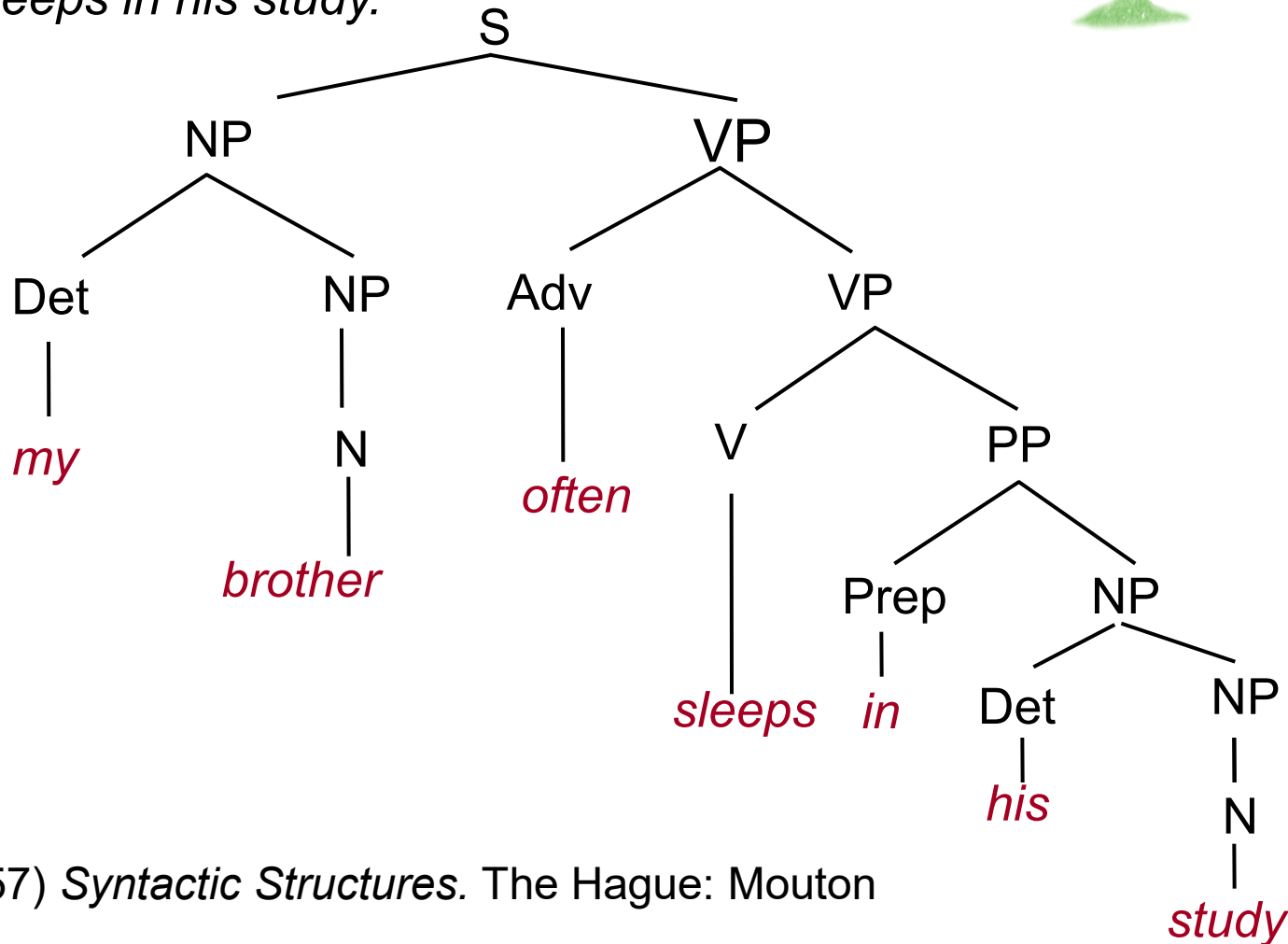
- phrase structure tree / constituent structure tree
- dependency tree



Phrase structure tree



My brother often sleeps in his study.



Noam Chomsky (1957) *Syntactic Structures*. The Hague: Mouton

Phrase structure tree (definition)



$T = \langle N, D, Q, P, L \rangle$

$\langle N, D \rangle$... **rooted tree, directed**

Q ... lexical and grammatical categories

L ... labeling function $N \rightarrow Q$

D ... oriented edges (branches)

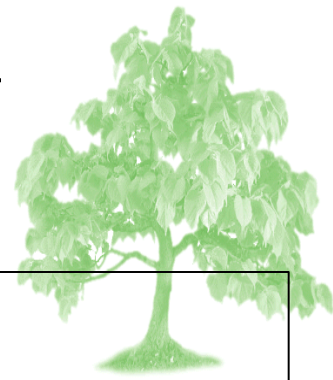
~ relation on lex. and gram. categories

dominance relation

+

P ... relation on N ~ (partial strong linear ordering)

relation of **precedence**



Phrase structure tree (definition)

$T = \langle N, D, Q, P, L \rangle$

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~ relation on lex. and gram. categories

dominance relation

+

P ... relation on N ~ (partial strong linear ordering)
relation of **precedence**

+

Relating dominance and precedence relations:

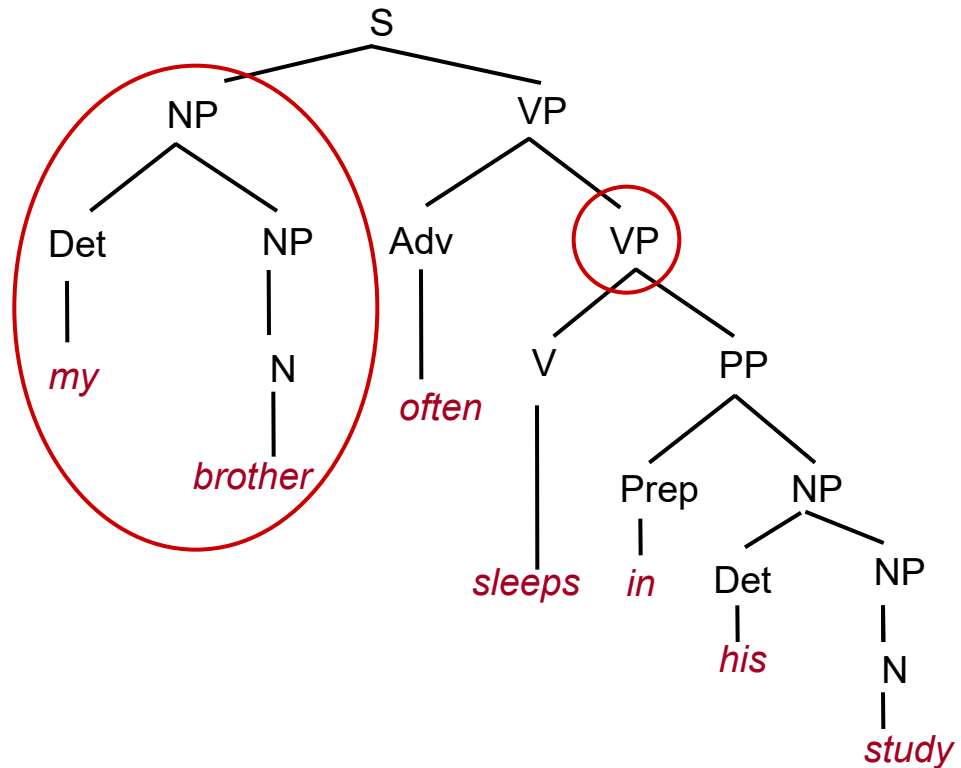
- **exclusivity** condition for D and P relations
- **'nontangling'** condition



Phrase structure tree (relation P)

- **exclusivity** condition for D and P relations

$\forall x,y \in N$ holds: $([x,y] \in P \vee [y,x] \in P) \Leftrightarrow ([x,y] \notin D \ \& \ [y,x] \notin D)$





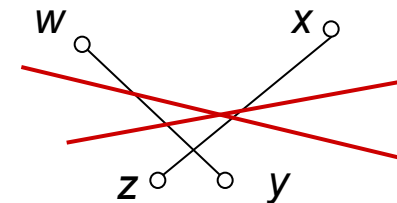
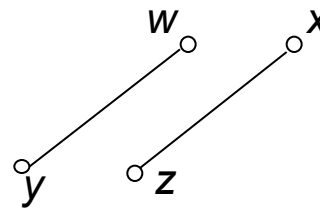
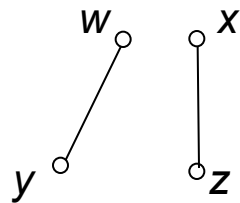
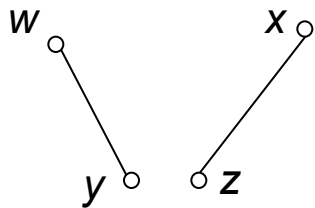
Phrase structure tree (relation P)

- **exclusivity** condition for D and P relations

$\forall x,y \in N$ holds: $([x,y] \in P \vee [y,x] \in P) \Leftrightarrow ([x,y] \notin D \ \& \ [y,x] \notin D)$

- **'nontangling'** condition

$\forall w,x,y,z \in N$ holds: $([w,x] \in P \ \& \ [w,y] \in D \ \& \ [x,z] \in D) \Rightarrow ([y,z] \in P)$





Phrase structure tree (relation P)

- *exclusivity* condition for D and P relations

$\forall x,y \in N$ holds: $([x,y] \in P \vee [y,x] \in P) \Leftrightarrow ([x,y] \notin D \ \& \ [y,x] \notin D)$

- *'nontangling'* condition

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 $\Rightarrow ([y,z] \in P)$



$T = \langle N, D, Q, P, L \rangle$ phrase structure tree

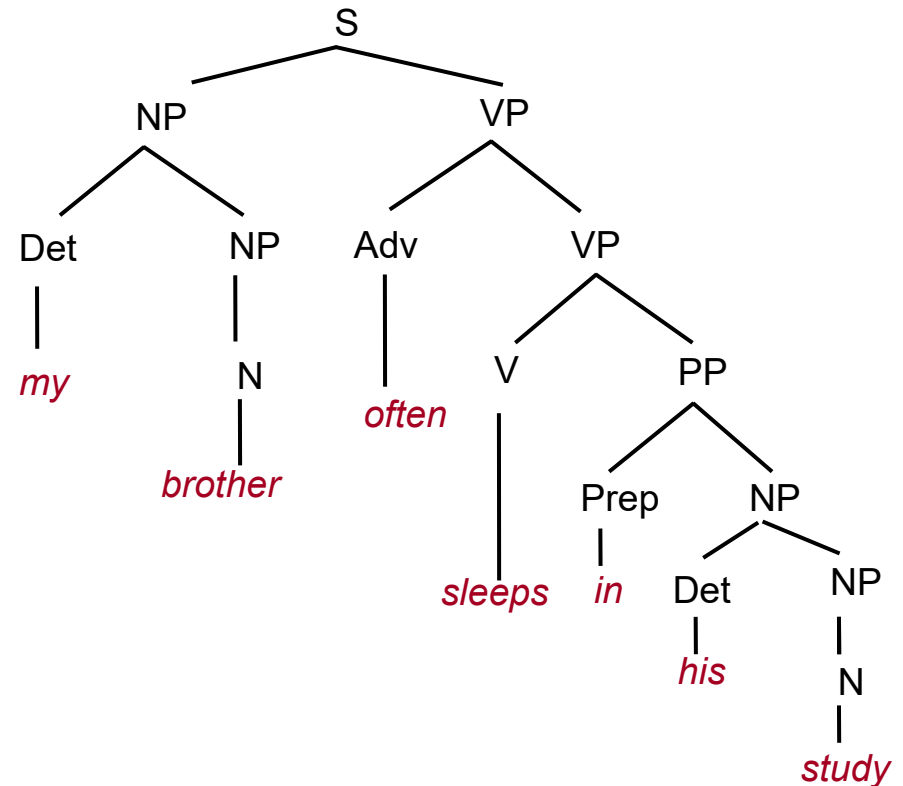
- $\forall x,y \in N$ siblings $\Rightarrow [x,y] \in P$
- the set of its leaves is totally ordered by P

Phrase structure tree



Pros

- derivation history / 'closeness' of a complementation
- **coordination**, apposition
- CFG-like
- derivation of a grammar

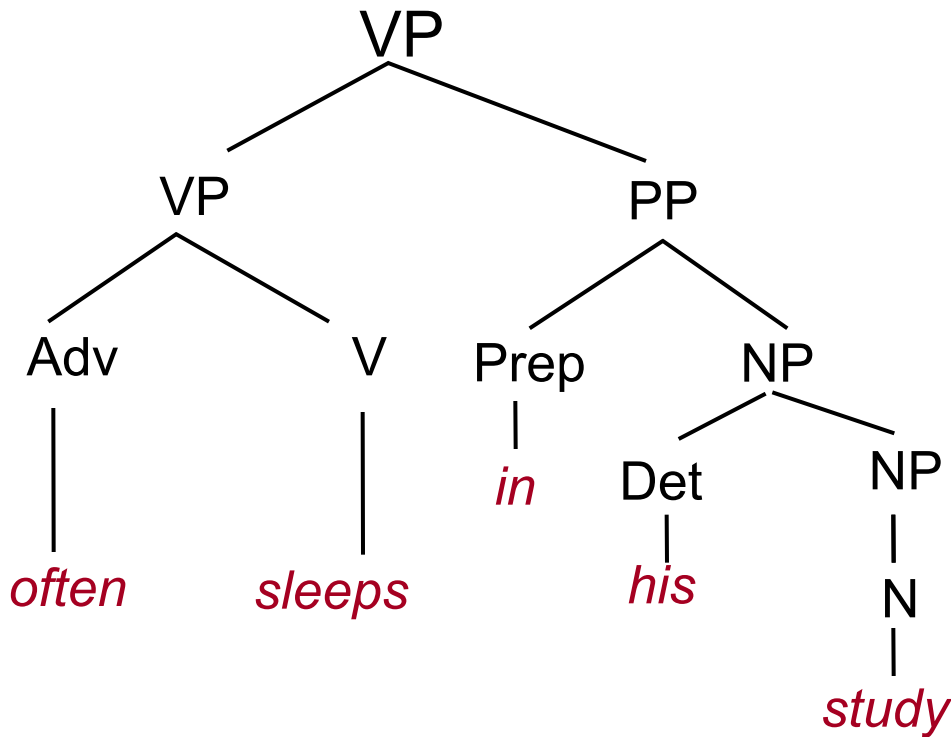




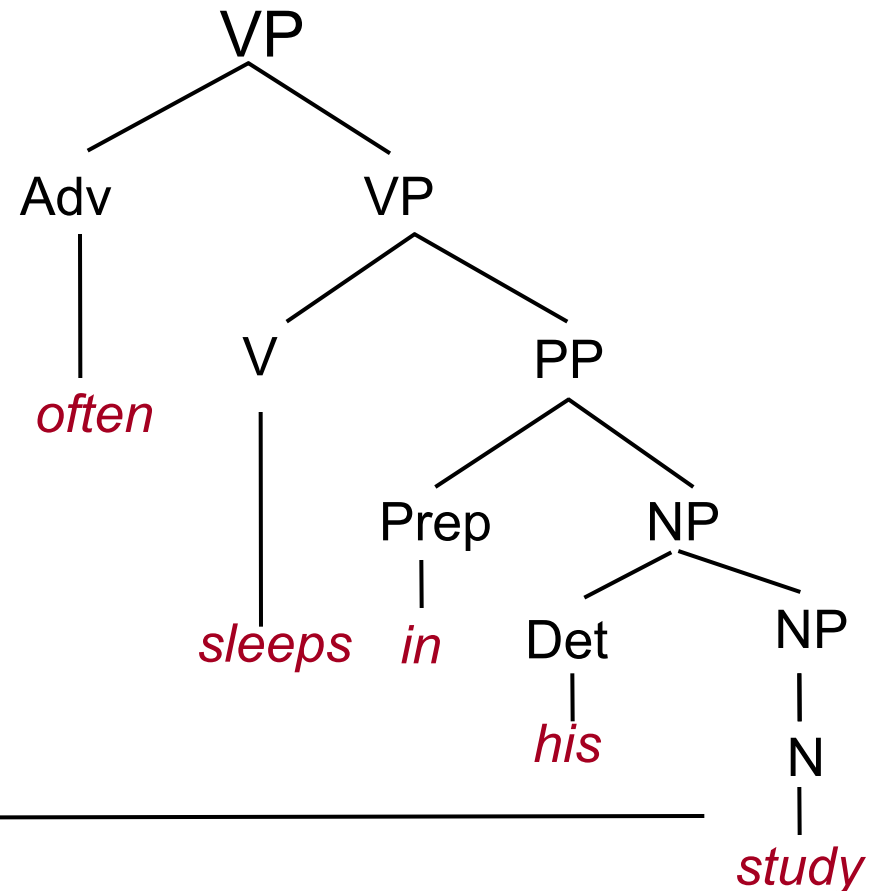
Phrase structure tree

derivation history / 'closeness':

... *often sleeps* in his study



... often *sleeps in his study*



Phrase structure tree



Pros

- derivation history / 'closeness' of a complementation
- **coordination**, apposition
- CFG-like
- derivation of a grammar

Contras

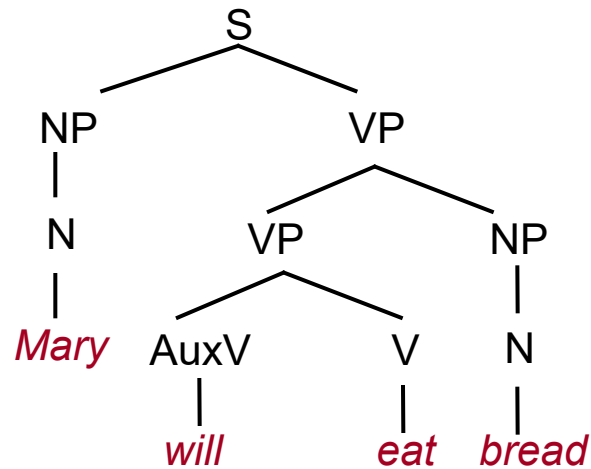
- complexity (number of non-terminal symbols)
- complement ('two dependencies')
přiběhl bos
[(he) arrived barefooted]
- **free word order**
discontinuous 'phrases'
non-projectivity



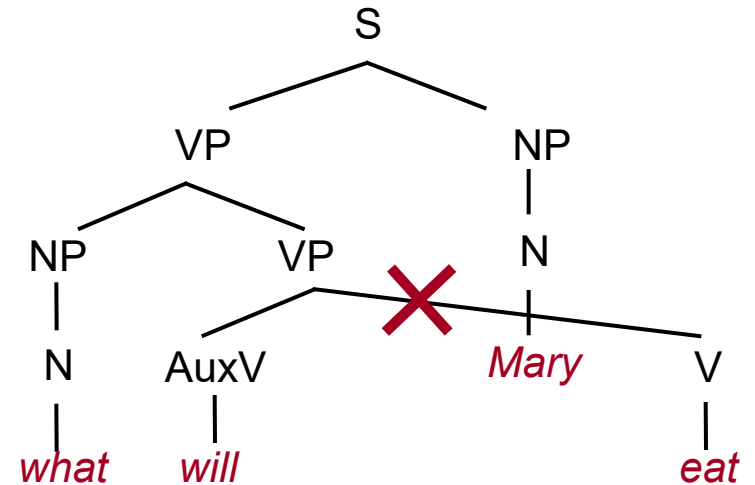
Phrase structure tree

discontinuous 'phrases': solution for English

Mary will eat bread.



What will Mary eat?



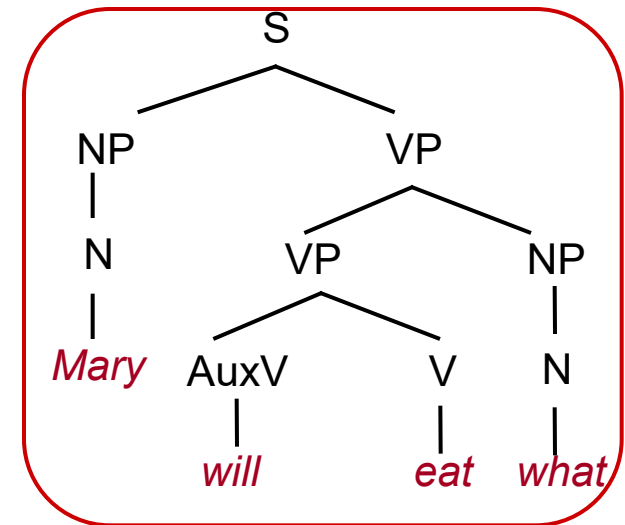
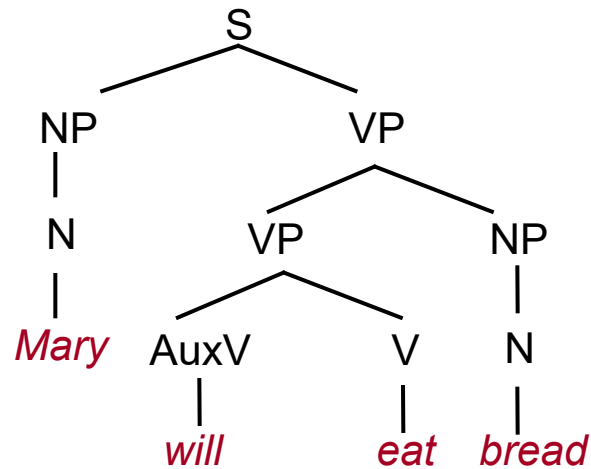


Phrase structure tree

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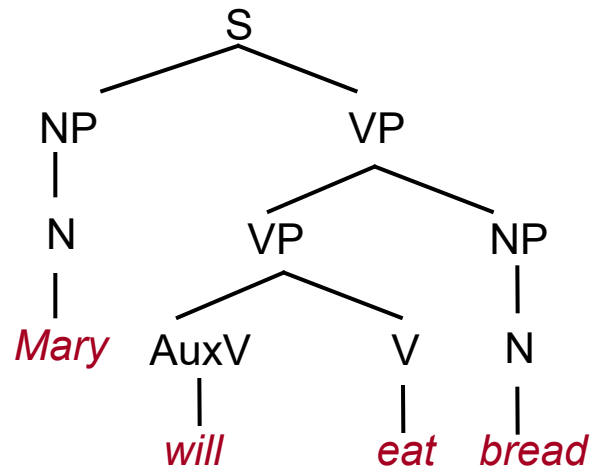




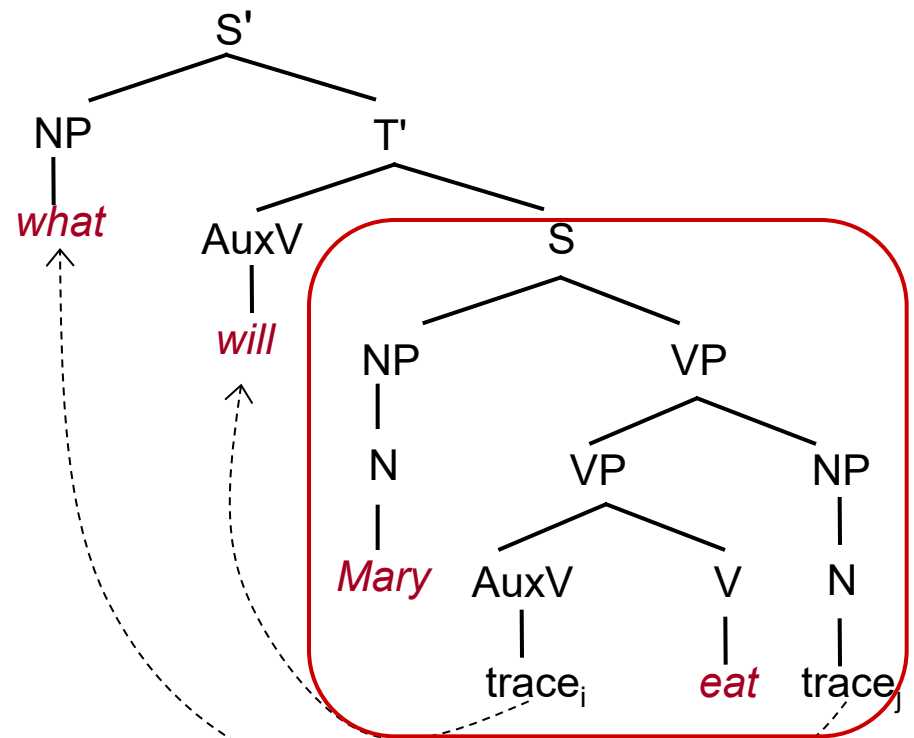
Phrase structure tree

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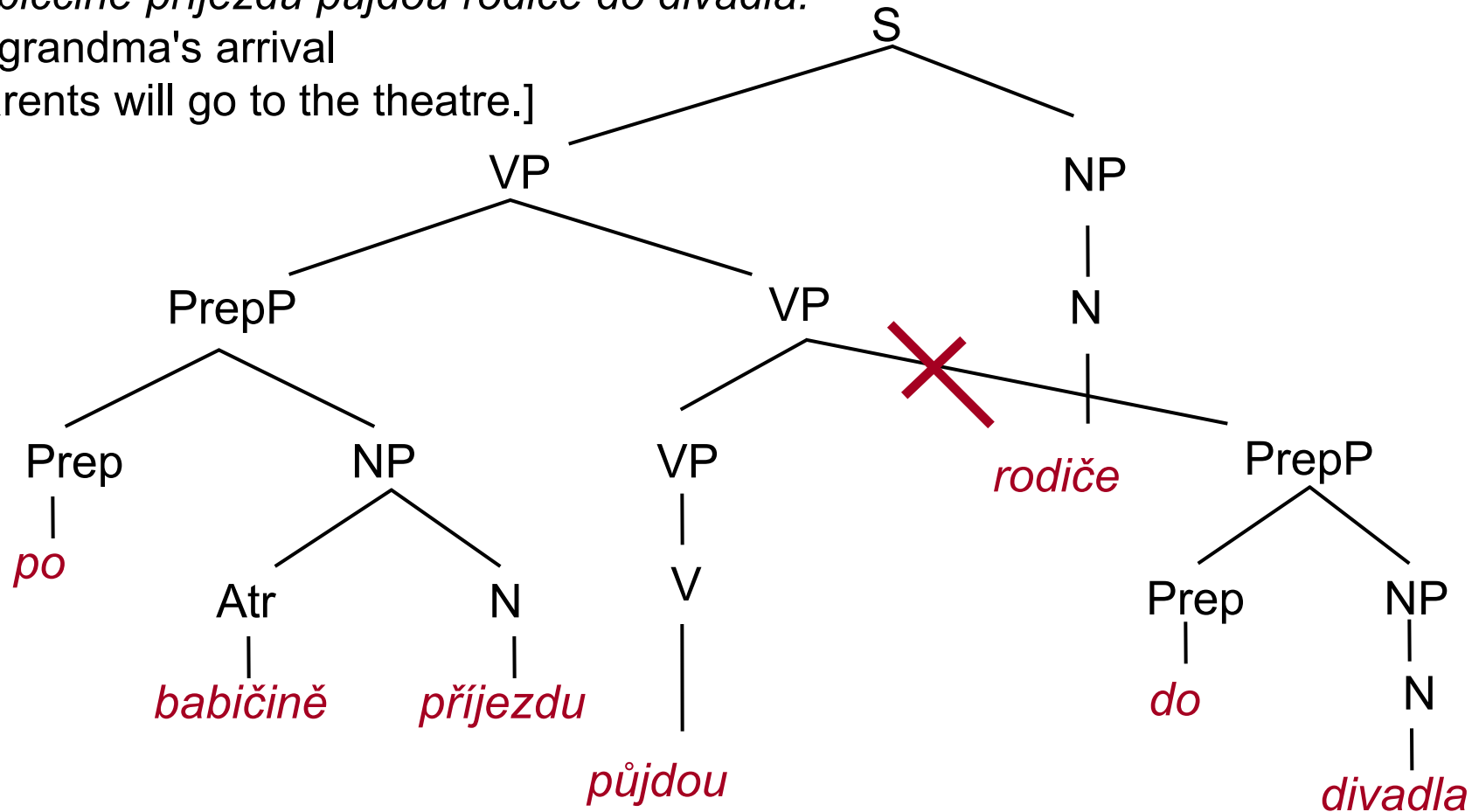




Phrase structure tree

discontinuous 'phrases':

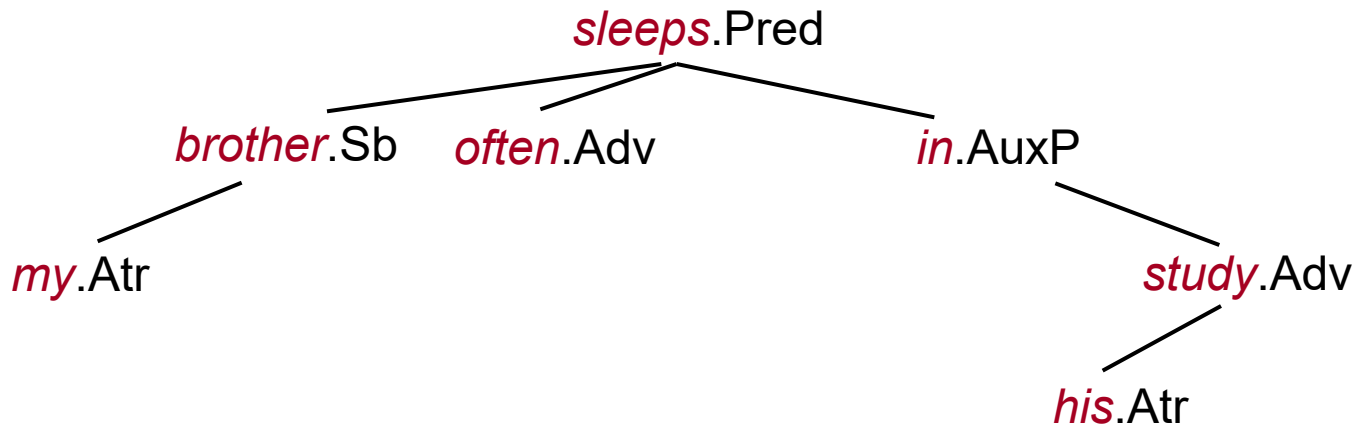
Po babiččině příjezdu půjdou rodiče do divadla.
[After grandma's arrival
the parents will go to the theatre.]



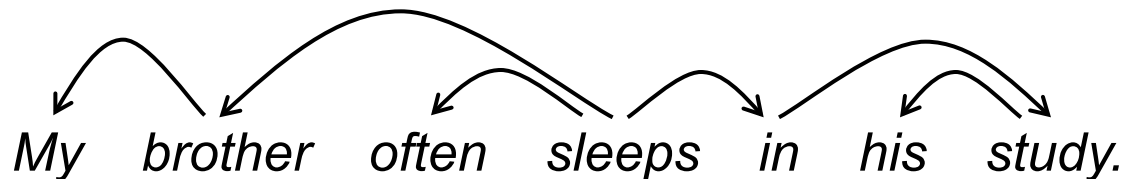
Dependency tree



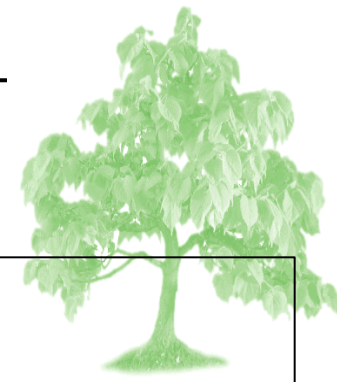
My brother often sleeps in his study.



Lucien Tesnière (1959) *Éléments de syntaxe structurale*. Editions Klincksieck.
Igor Mel'čuk (1988) *Dependency Syntax: Theory and Practice*. State University of New York Press.



My brother often sleeps in his study.



Dependency tree (definition)

$T = \langle N, D, Q, WO, L \rangle$

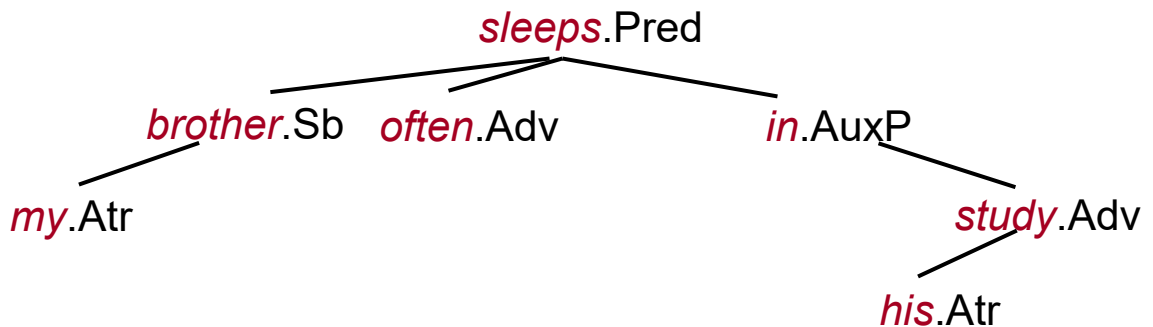
$\langle N, D \rangle$... **rooted tree, directed**

Q ... lexical and grammatical categories

L ... labeling function $N \rightarrow Q^+$

D ... oriented edges \sim relation on lex. and gram. categories
'dependency' relation

WO ... relation on N \sim (strong total ordering on N) ...
word order





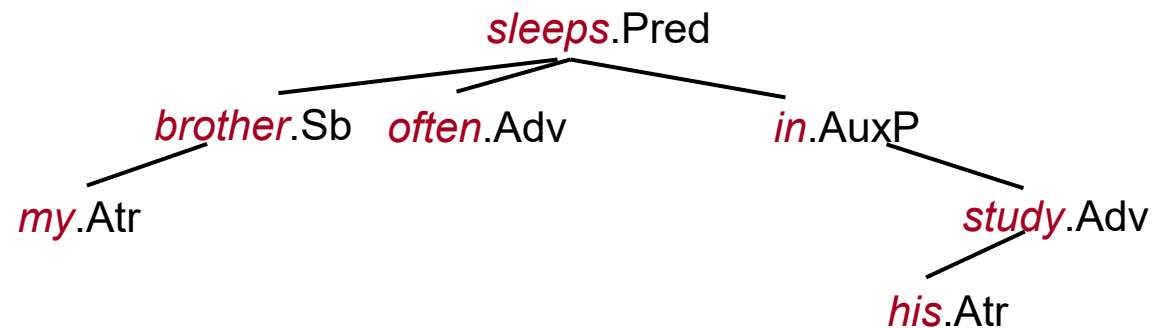
Dependency tree

Pros

- economical, clear
(complex labels, 'word'~ node)
- **free word order**
- head of a phrase

Contras

- no derivation history /
'closeness'
- **coordination**, apposition
- complement



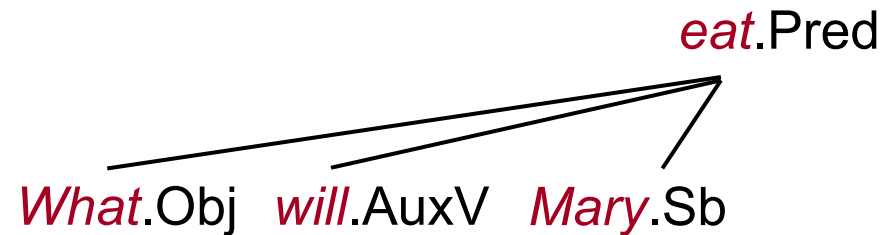
Dependency tree



discontinuous 'phrases': no problem

Mary will eat bread.

What will Mary eat?

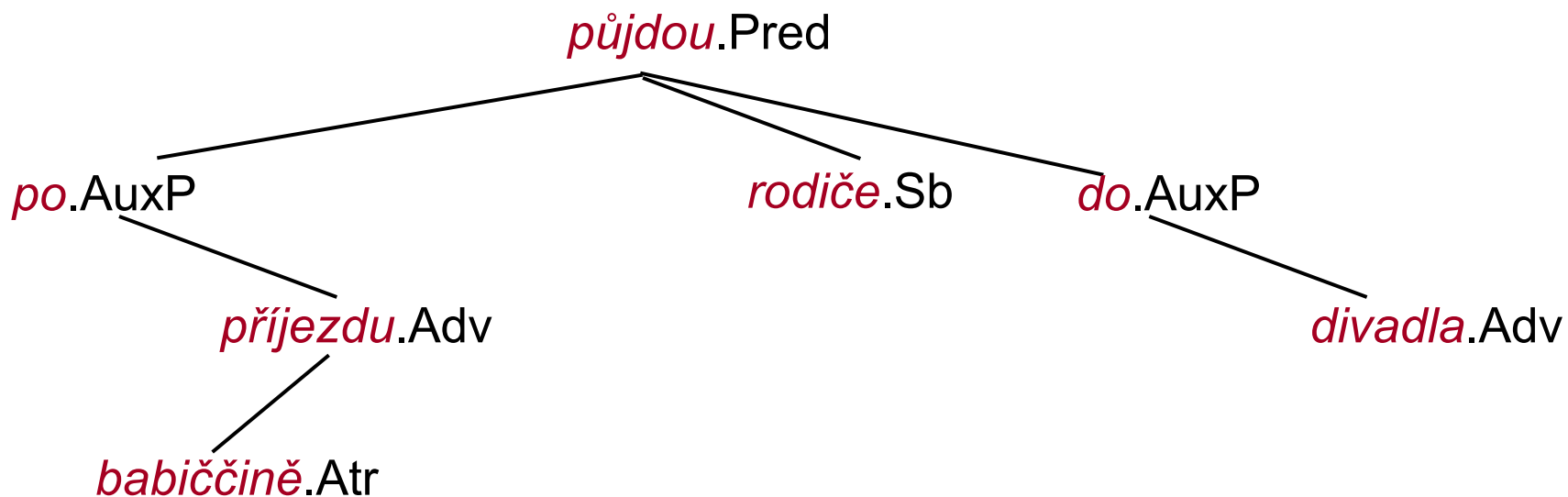


Dependency tree

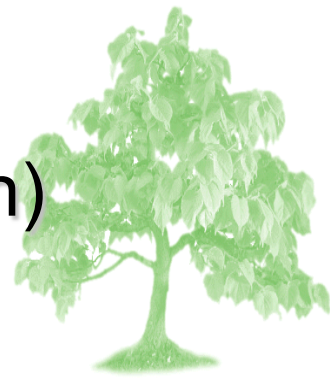


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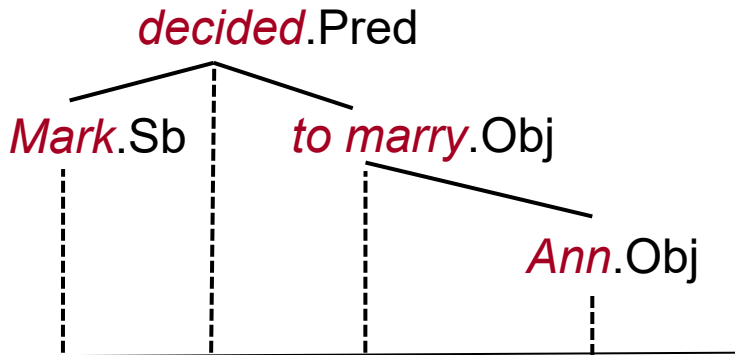
[After grandma's arrival the parents will go to the theatre.]



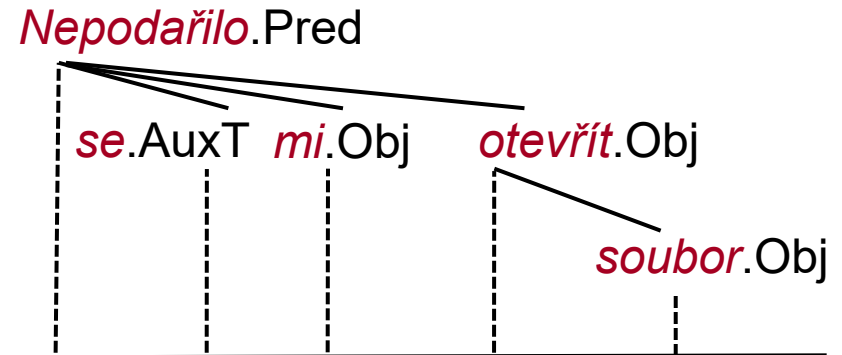
Projectivity and non-projectivity (definition)



Mark decided to marry Ann.



Nepodařilo se mi otevřít soubor.

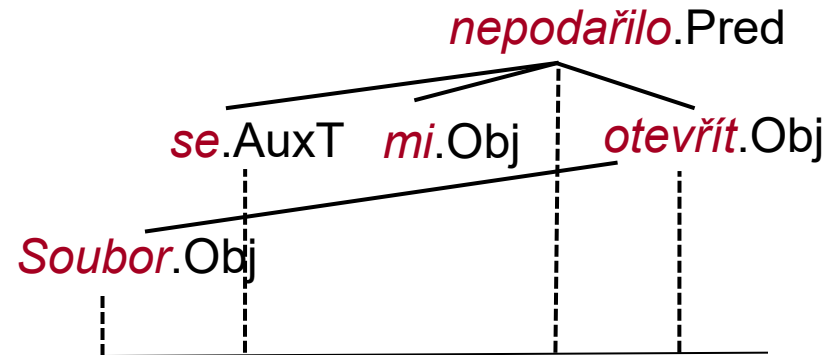
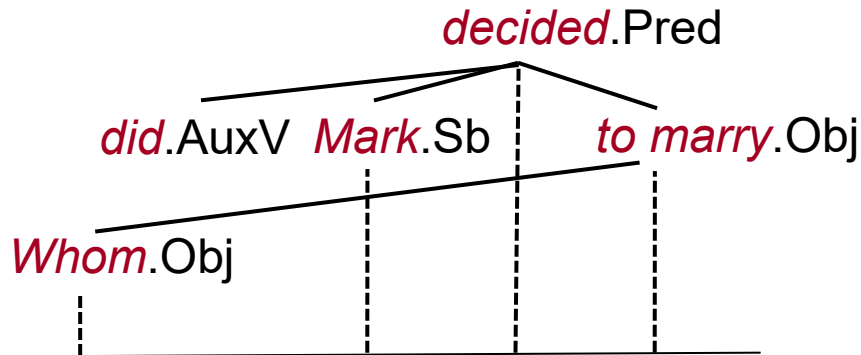


Projectivity and non-projectivity (definition)

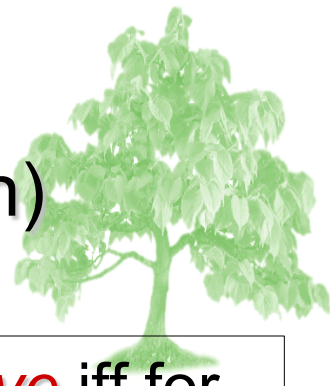


Whom did Mark decided to marry?

Soubor se mi nepodařilo otevřít. (Oliva)



Projectivity and non-projectivity (definition)

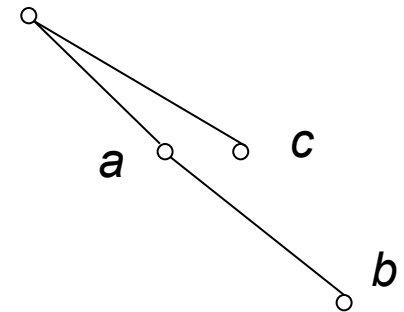
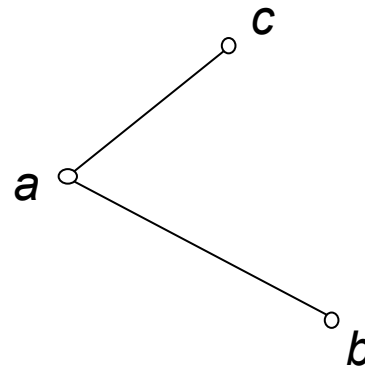
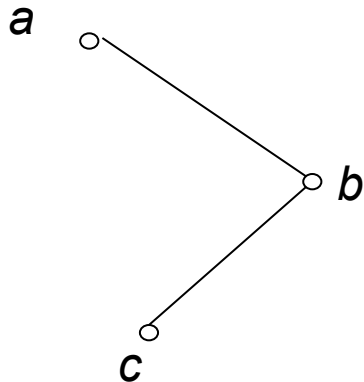
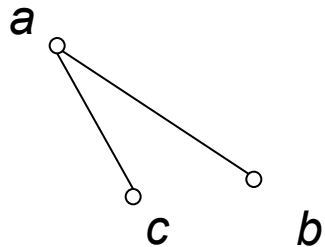


A subtree S of a rooted dependency tree T is *projective* iff for all nodes a , b and c of the subtree S the condition holds:

$$(1) (a \leq_D b) \ \& \ (a <_{WO} c <_{WO} b) \Rightarrow (a <_D^* c)$$

and

$$(2) (a \leq_D b) \ \& \ (b <_{WO} c <_{WO} a) \Rightarrow (a <_{WO}^* c)$$



Projectivity and free word order



free word order:

- freedom of word order of dependents within a continuous ‘head domain’ (i.e., substring of head + its dependents)
- relaxation of continuity of a head domain

German:

Maria hat einen Mann kennengelernt der Schmetterlinge sammelt.

Mary has a man met the butterflies collects

‘Mary has met a man who collects butterflies.’

English: long-distance unbounded dependency

John, Peter thought that Sue said that Mary loves.

Czech:

Marii se Petr tu knihu rozhodl nekoupit.

to-Mary PART Peter that book decided not-buy

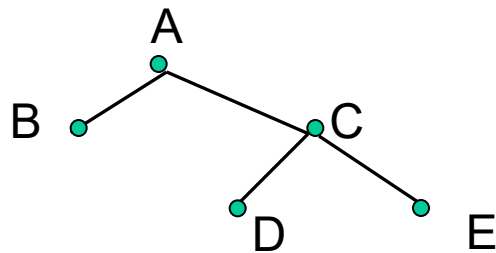
‘Peter decided not to buy that book to Mary.’

Projectivity and non-projectivity

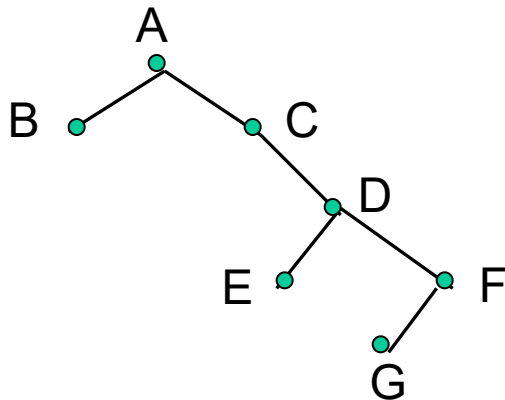


Projective dependency trees can be encoded by *linearization*:

- string of nodes, edges ~ brackets

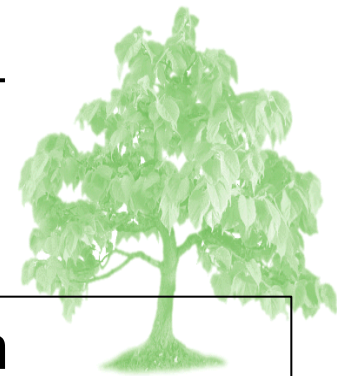


$A(B C (D E))$ without WO ordering
 $(B)A((D)C(E))$ with WO



$A(B C (D (E F (G))))$ without WO
 $(B)A(C((E)D((G)F)))$ with WO

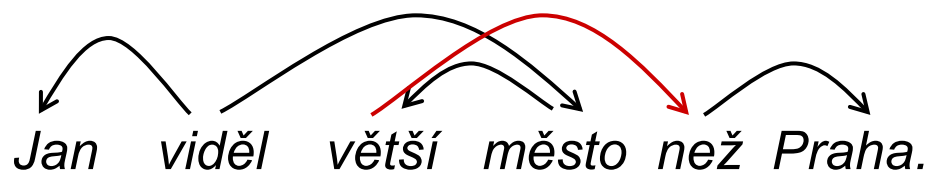
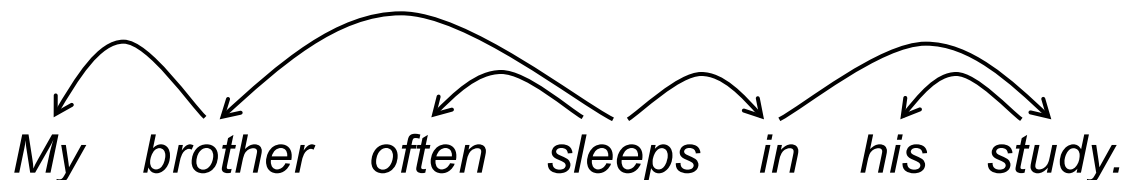
Planarity



A dependency graph T is *planar*, if it does *not* contain nodes a, b, c, d such that:

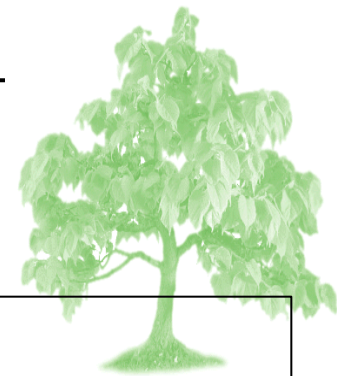
$$\textit{linked}(a,c) \ \& \ \textit{linked}(b,d) \ \& \ a \prec_{\text{WO}} b \prec_{\text{WO}} c \prec_{\text{WO}} d$$

linked(i,j) ... ‘there is an edge in T from i to j , or vice versa’



Informally, a dependency graph is planar, if its edges can be drawn above the sentence without crossing.

Planarity vs. projectivity



projectivity \Rightarrow planarity

projectivity \nLeftarrow planarity

(Kuhlmann, M., Nivre, J., 2006)

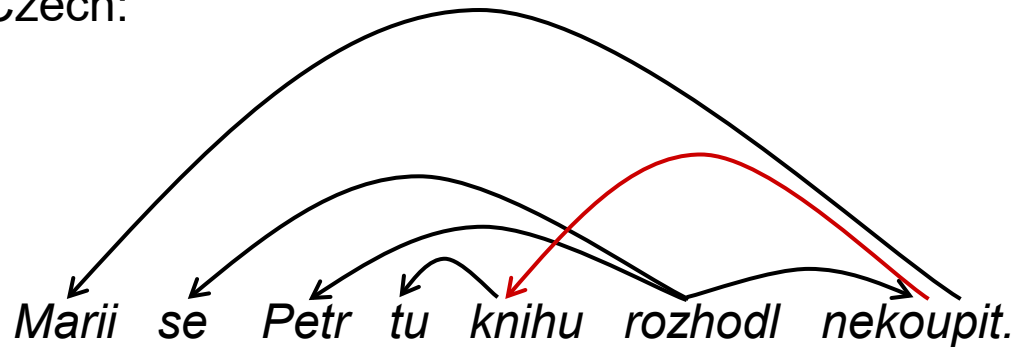
Soubor se mi nepodařilo otevřít.

A diagram consisting of five curved arrows pointing downwards from the text above to the words in the sentence below. The arrows originate from the space between 'projectivity' and 'planarity' in the first two lines and point to the words 'Soubor', 'se', 'mi', 'nepodařilo', and 'otevřít.' respectively.

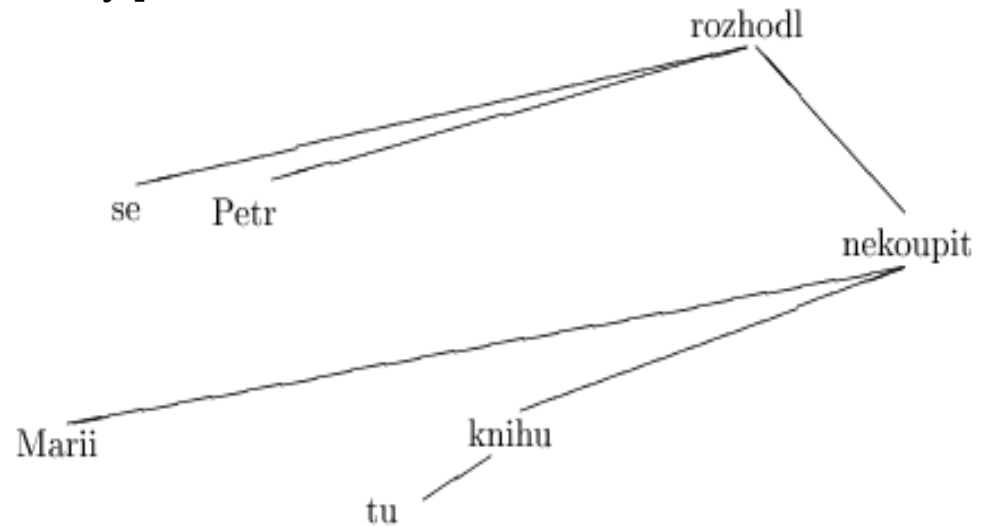
Projectivity and free word order



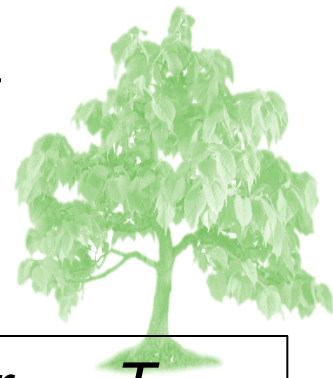
Czech:



to-Mary PART Peter that book decided not-buy
[Peter decided not to buy that book to Mary.]



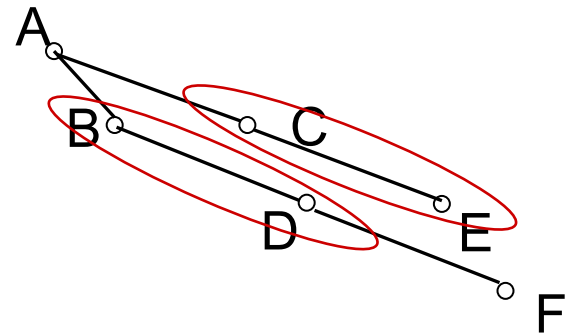
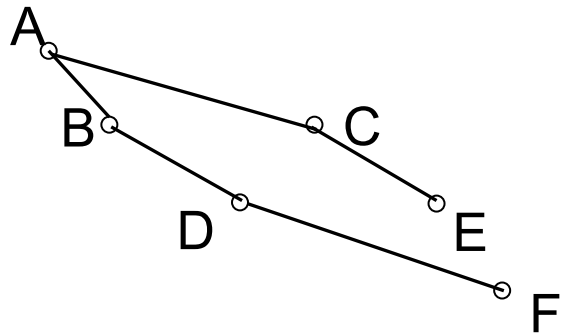
'Well-Nestedness'



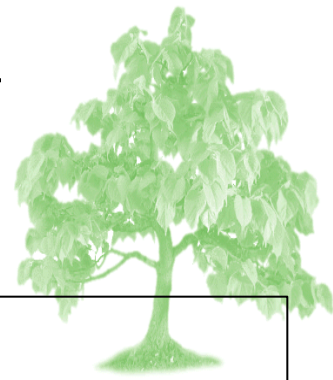
Two subtrees T_1, T_2 *interleave*, if there are nodes $l_1, r_1 \in T_1$ and $l_2, r_2 \in T_2$ such that

$$l_1 <_{WO} l_2 <_{WO} r_1 <_{WO} r_2$$

A dependency graph is *well-nested*, if no two of its disjoint subtrees interleave.'



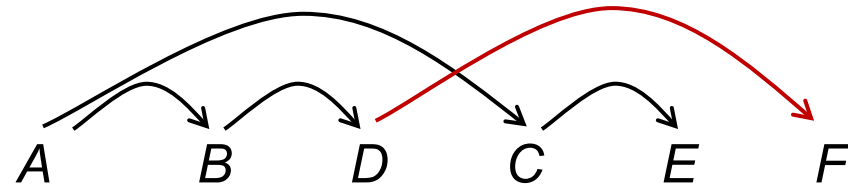
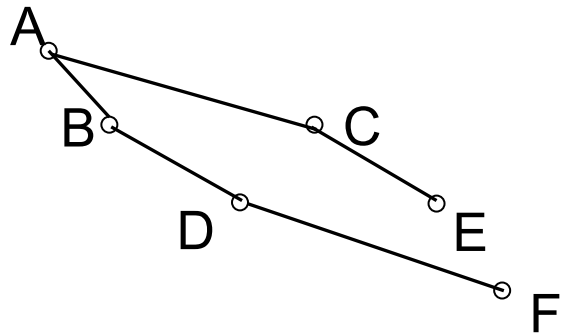
Planarity vs. projectivity



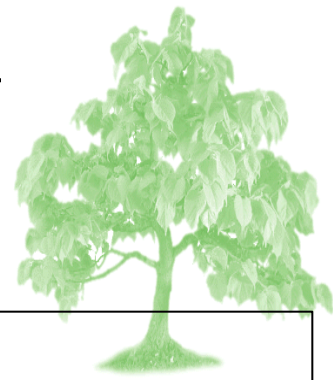
projectivity \Rightarrow planarity \Rightarrow well-nestedness

projectivity $\not\Leftarrow$ planarity $\not\Leftarrow$ well-nestedness

(Kuhlmann, M., Nivre, J., 2006)



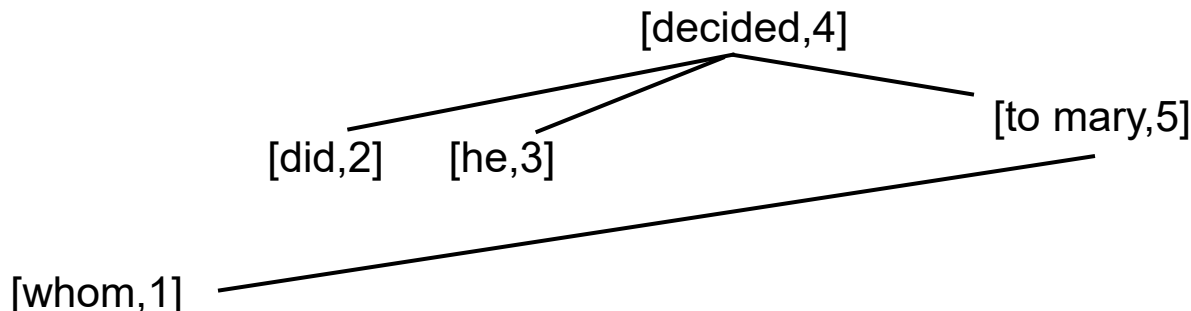
Gap Degree $dNh(T)$



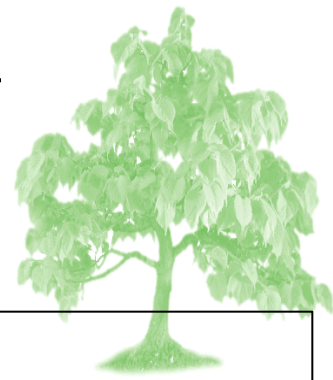
Coverage of a node $u \in T$

$Cov(u, T) = \{ i \mid i \text{- word order position of } v \in T \text{ such that, } u \leq_D v \}$

$Cov(u_1, T) = \{ 1 \}; Cov(u_2, T) = \{ 2 \}; Cov(u_3, T) = \{ 3 \}; Cov(u_4, T) = \{ 1, 2, 3, 4, 5 \}; Cov(u_5, T) = \{ 1, 5 \}$



Gap Degree $dNh(T)$



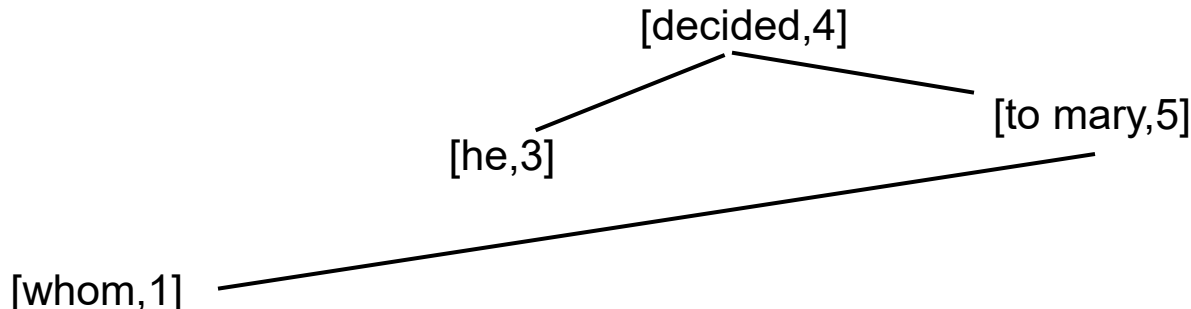
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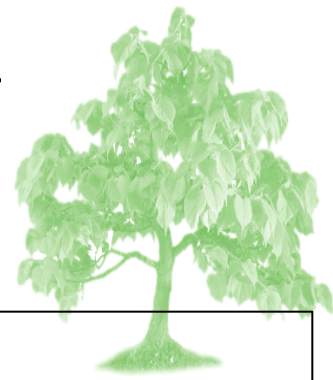
Gap in Coverage of a node $u \in T \Leftrightarrow_{\text{def}} Cov(u, T)$ is not an interval

$dNh(u, T)$... **number of Gaps** in $Cov(u, T)$

$Cov(u_1, T) = \{ 1 \}$; $Cov(u_2, T) = \{ 2 \}$; $Cov(u_3, T) = \{ 3 \}$; $Cov(u_4, T) = \{ 1, 2, 3, 4, 5 \}$; $Cov(u_5, T) = \{ 1, 5 \}$



Gap Degree $dNh(T)$



Coverage of a node $u \in T$

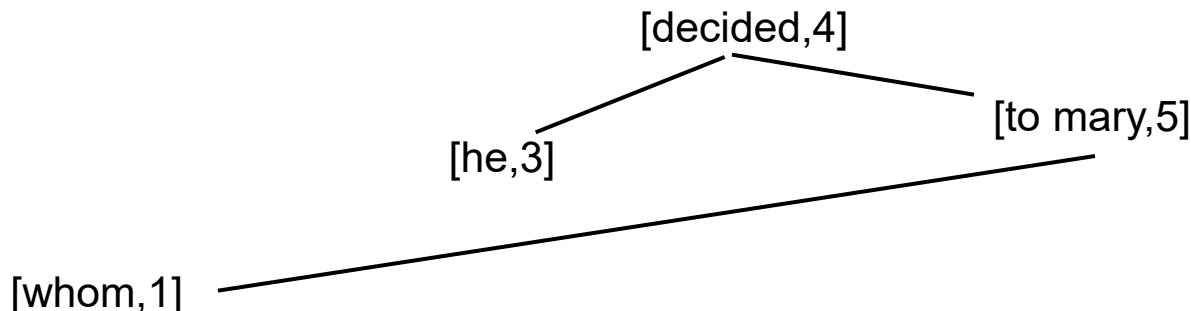
$Cov(u, T) = \{ i \mid i \text{ - word order position of } v \in T \text{ such that, } u \leq_D v \}$

Gap in Coverage of a node $u \in T \Leftrightarrow_{\text{def}} Cov(u, T)$ is not an interval

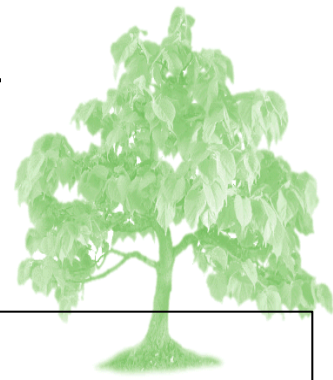
$dNh(u, T)$... **number of Gaps** in $Cov(u, T)$

Tree Gap Degree $dNh(T) = \max \{ dNh(u, T) \mid u \in T \}$

$Cov(u_1, T) = \{ 1 \}$; $Cov(u_2, T) = \{ 2 \}$; $Cov(u_3, T) = \{ 3 \}$; $Cov(u_4, T) = \{ 1, 2, 3, 4, 5 \}$; $Cov(u_5, T) = \{ 1, 5 \}$



Gap Degree $dNh(T)$



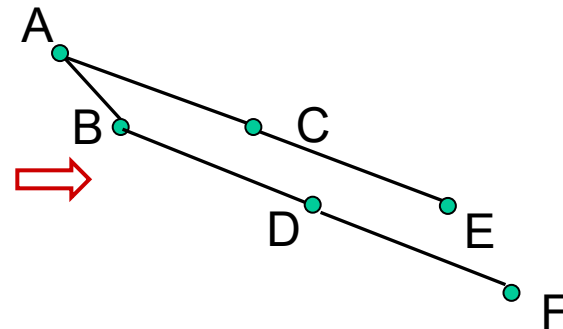
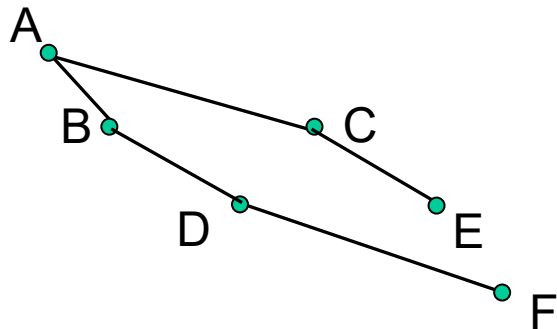
Coverage of a node $u \in T$

$Cov(u, T) = \{ i \mid i \text{ - word order position of } v \in T \text{ such that, } u \leq_D v \}$

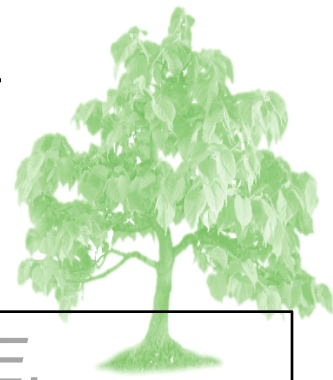
Gap in Coverage of a node $u \in T \Leftrightarrow_{\text{def}} Cov(u, T)$ is not an interval

$gd(u, T)$... **number of Gaps** in $Cov(u, T)$

Tree Gap Degree $gd(T) = \max \{gd(u, T) \mid u \in T\}$



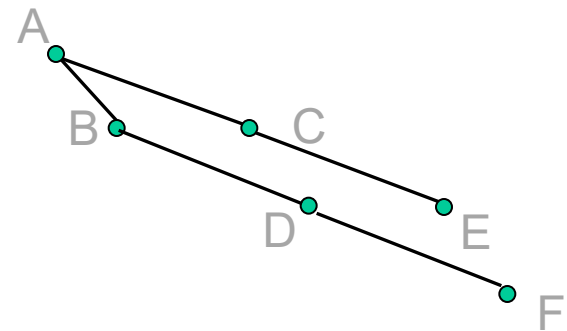
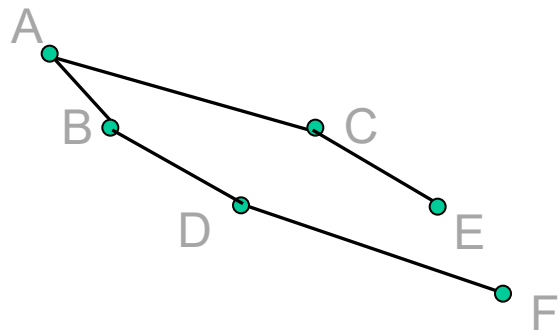
Edge Degree



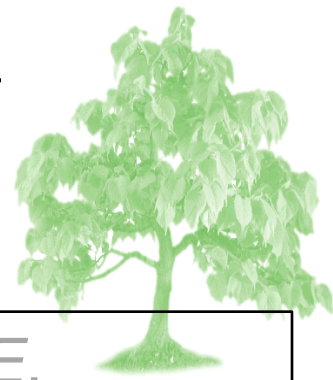
Let $T = (N, E)$ dependency tree, $e = [i, j]$ an edge in E , T_e the subgraph of T induced by the nodes contained in the span of e .

Degree of an edge $e \in E$, $ed(e)$, is the number of connected components c in T_e such that the root of c is not dominated by the head of e .

Edge degree of T , $ed(T) \dots \max \{ed(e) \mid e \in T\}$



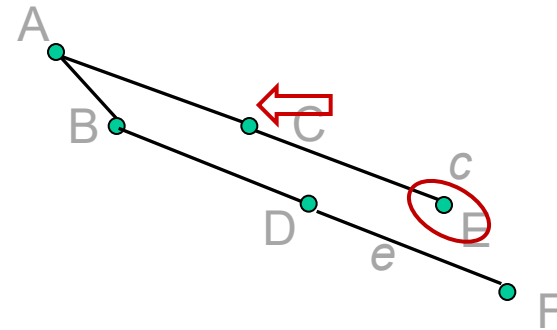
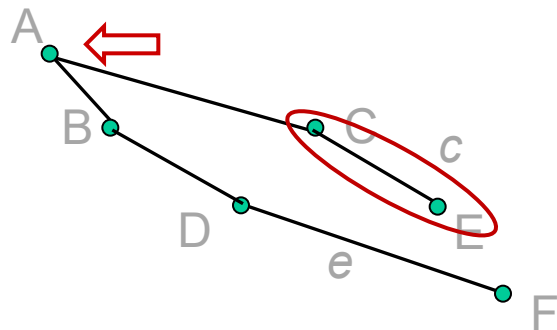
Edge Degree

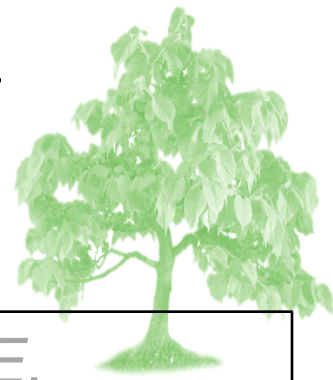


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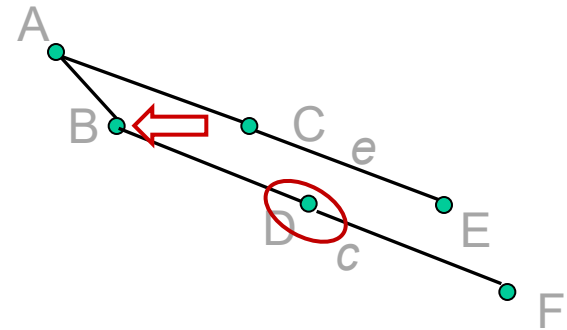
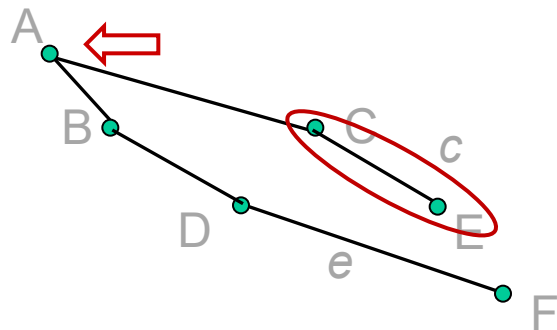


Edge Degree

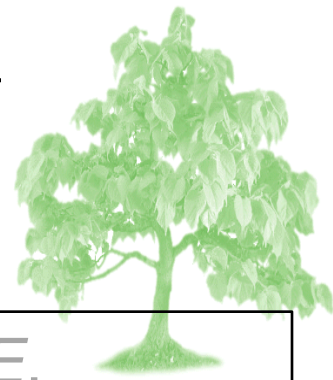
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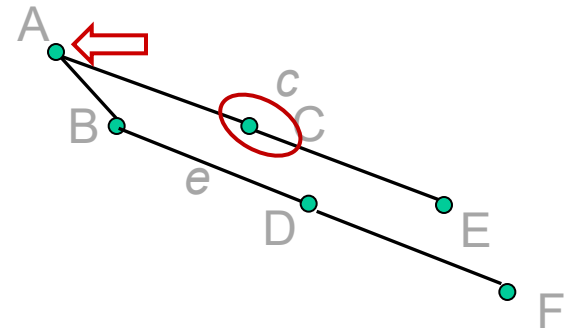
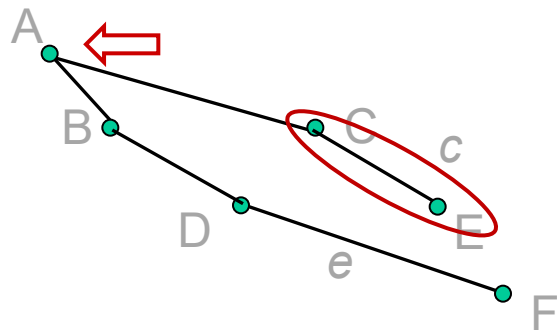
Edge Degree



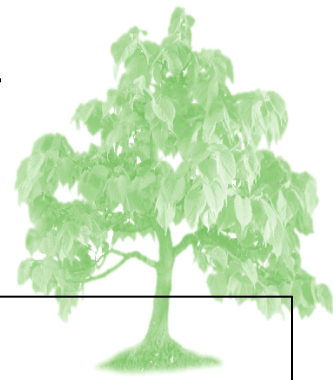
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Edge degree of T , $ed(T) \dots \max \{ed(e) \mid e \in T\}$



Planarity vs. projectivity



projectivity \Rightarrow planarity \Rightarrow well-nestedness

projectivity $\not\Leftarrow$ planarity $\not\Leftarrow$ well-nestedness

$gd(T) = 0 \Leftrightarrow ed(T) = 0 \Leftrightarrow$ projectivity

well-nestedness ... independent from gap/edge degree

$\forall d > 0$ well-nested and non-well-nested trees exist such that $gd(T) = d$ and $ed(T) = d$

(Kuhlmann, M., Nivre, J., 2006)

| property | DDT | | PDT | |
|---------------------------------------|------------|--------|-------------|---------|
| <i>all structures</i> | $n = 4393$ | | $n = 73088$ | |
| gap degree 0 | 3732 | 84.95% | 56168 | 76.85% |
| gap degree 1 | 654 | 14.89% | 16608 | 22.72% |
| gap degree 2 | 7 | 0.16% | 307 | 0.42% |
| gap degree 3 | – | – | 4 | 0.01% |
| gap degree 4 | – | – | 1 | < 0.01% |
| edge degree 0 | 3732 | 84.95% | 56168 | 76.85% |
| edge degree 1 | 584 | 13.29% | 16585 | 22.69% |
| edge degree 2 | 58 | 1.32% | 259 | 0.35% |
| edge degree 3 | 17 | 0.39% | 63 | 0.09% |
| edge degree 4 | 2 | 0.05% | 10 | 0.01% |
| edge degree 5 | – | – | 2 | < 0.01% |
| edge degree 6 | – | – | 1 | < 0.01% |
| projective | 3732 | 84.95% | 56168 | 76.85% |
| planar | 3796 | 86.41% | 60048 | 82.16% |
| well-nested | 4388 | 99.89% | 73010 | 99.89% |
| <i>non-projective structures only</i> | $n = 661$ | | $n = 16920$ | |
| planar | 64 | 9.68% | 3880 | 22.93% |
| well-nested | 656 | 99.24% | 16842 | 99.54% |



Corpora with dependency trees

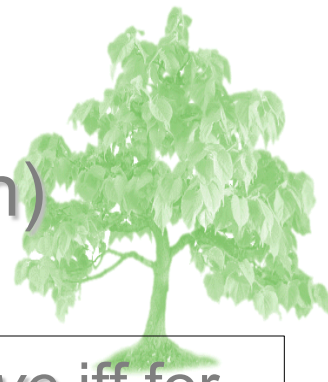


- PropBank (1995)
<http://propbank.github.io/>
 - family of Prague dependency treebanks: Czech, Arabic, English, ...
<http://ufal.mff.cuni.cz/pdt.html>
 - HamleDT project (from 2012) <http://ufal.mff.cuni.cz/hamledt>
 - **Universal Dependencies** (from 2013) <http://universaldependencies.org/>
 - Danish Dep. Treebank
<http://mbkromann.github.io/copenhagen-dependency-treebank/>
 - Finnish: Turku Dependency Treebank
<http://bionlp.utu.fi/fintreebank.html>
 - Negra corpus
<http://www.coli.uni-saarland.de/projects/sfb378/negra-corpus/negra-corpus.html>
 - TIGERCorpus
<http://www.ims.uni-stuttgart.de/forschung/ressourcen/korpora/tiger.html/>
 - SynTagRus Dependency Treebank for Russian
-



References

- Partee, B. H.; ter Meulen, A.; Wall, R. E. (1990) *Mathematical Methods in Linguistics*. Kluwer Academic Publishers
 - Kuhlmann, M., Nivre, J. (2006) Mildly Non-Projective Dependency Structures. In COLING/ACL Main Conference Poster Sessions, 507–514.
 - Havelka, J. (2007) Mathematical Properties of Dependency Trees and their Application to Natural Language Syntax. PhD Thesis, MFF UK
 - Holan, T., Kuboň, V., Oliva, K., Plátek, M. (2000) On Complexity of Word Order. *Les grammaires de dépendance – Traitement automatique des langues*, vol. 41, no. 1, 273-300
 - Petkevič, V. (1995) A New Formal Specification of Underlying Structure. *Theoretical Linguistics*, vol. 21, No.1
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Projectivity and non-projectivity (definition)

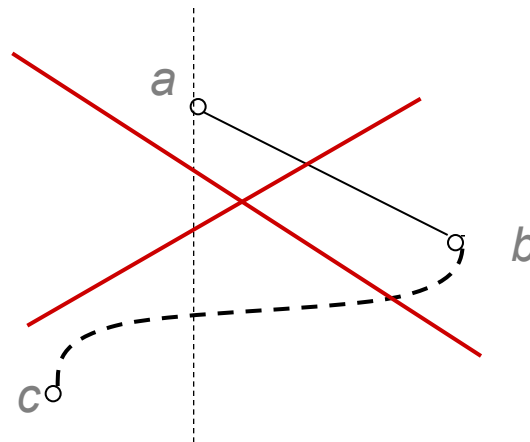
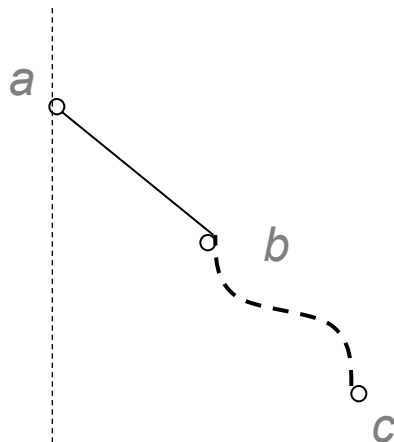
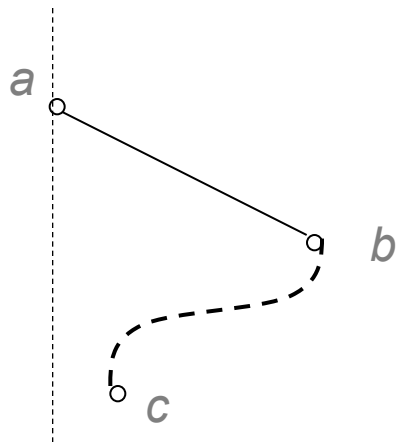
NENÍ ekvivalentní podmínka, viz Jura PhD, str. 30 !!!

A subtree S of a rooted dependency tree T is *projective* iff for all nodes a , b and c of the subtree S the condition holds:

$$(1) (a \leq_D b) \ \& \ (a <_{WO} b) \ \& \ (b \leq_D^* c) \ \Rightarrow \ (a <_{WO} c)$$

and

$$(2) (a \leq_D b) \ \& \ (b <_{WO} a) \ \& \ (b \leq_D^* c) \ \Rightarrow \ (c <_{WO} a)$$



counter-example:

